

Faculty of Computer Science 

Institute of Theoretical Computer Science

Chair of Automata Theory

# COMPUTING OPTIMAL REPAIRS OF QUANTIFIED ABOXES W.R.T. STATIC $\mathcal{EL}$ TBOXES

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**Rules:**  $\mathcal{EL}$  TBox  $\mathcal{T}$ 

 $\mathcal{EL} \text{ concepts:}$   $C ::= \top \mid A \mid C \sqcap C \mid \exists r. C$ where  $A \in \Sigma_{\mathsf{C}}$  and  $r \in \Sigma_{\mathsf{R}}$   $\mathcal{EL} \text{ concept inclusions:}$   $C_1 \sqsubseteq C_2$ 

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# syntax independent

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#### **Repair Recipe**

 $\mathsf{Conj}(C_1 \sqcap C_2 \sqcap \cdots \sqcap C_n) = \{C_1, C_2, \dots, C_n\}$ 

**Repair Recipe:** For each unwanted consequence C(u):

- either choose a concept name  $B \in Conj(C)$  and remove B(u) from A,
- or choose an existential restriction  $\exists r. D \in Conj(C)$  and do the following for each  $r(u, v) \in A$ :
  - if  $D \neq \top$ , then recursively modify  $\mathcal{A}$  such that it does not entail D(v),
  - otherwise, remove r(u, v) from  $\mathcal{A}$ .

#### Taking the TBox into Account

#### **Forward Chaining:**

In order to not lose consequences that follow from removed axioms, but that do not itself violate the repair request, we initially need to **saturate** the qABox by means of the axioms in the TBox.

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- We consider CQ-entailment (which here coincides with classical entailment), and IQ-entailment.

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#### **Backward Chaining:**

- When removing an atomic unwanted consequence B(u) or  $\exists r. D(u)$ , it is also necessary to remove all E(u) where  $E \sqsubseteq_{\mathcal{T}} B$  or  $E \sqsubseteq_{\mathcal{T}} \exists r. D$ , respectively.
- It suffices to consider concepts  $E \in Sub(\mathcal{T}, \mathcal{R})$ .

#### **Canonical Repairs**

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#### **Main Results:**

- Given a qABox, a cycle-restricted TBox, and a repair request, the set of all optimal CQ-repairs can be computed in exponential time using an NP-oracle.
- Given a qABox, a TBox, and a repair request, the set of all optimal IQ-repairs can be computed in exponential time.

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- There are examples where an optimal repair need not be exponentially large.
- In these cases, the canonical repair is already equivalent to a small sub-qABox.
- We propose a rule-based approach to computing **optimized repairs**, which contain only relevant parts of the canonical repairs.

### That's it for now!

## Do you have questions or comments?

# See also our poster for further details.