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Measurement of Hg-197 and Hg-197m by a dose calibrator

R. Freudenberg, M. Vogel, M. Andreeff, J. Kotzerke



DRESDEN
concept
Exzellenz aus
Wissenschaft
und Kultur

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Motivation

Hg-197 and Hg-197m

- **promising for future application** in nuclear medicine:
 - low energy gamma radiation for imaging
 - Auger and conversion electrons for therapy
- simultaneously **produced by proton irradiation of natural gold** using a cyclotron

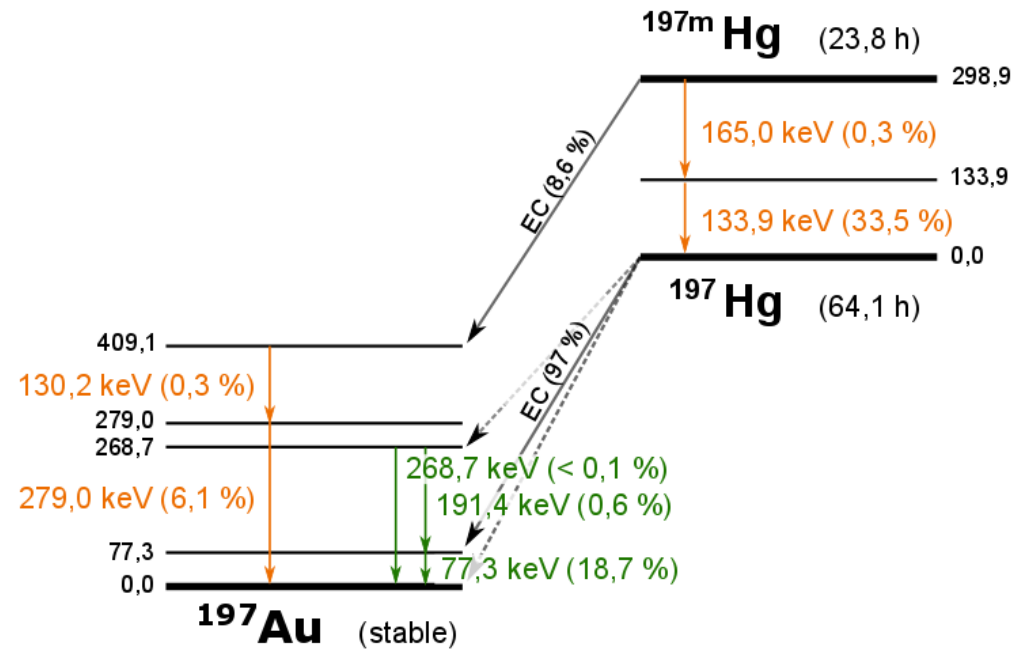


Fig. 1: Decay scheme of Hg-197(m) showing the major photon emissions.

Data from: Nuclear Data Sheets for A = 197 (2004)

Motivation

Hg-197 and Hg-197m

- **promising for future application** in nuclear medicine:
 - low energy gamma radiation for imaging
 - Auger and conversion electrons for therapy
- **simultaneously produced by proton irradiation of natural gold** using a cyclotron

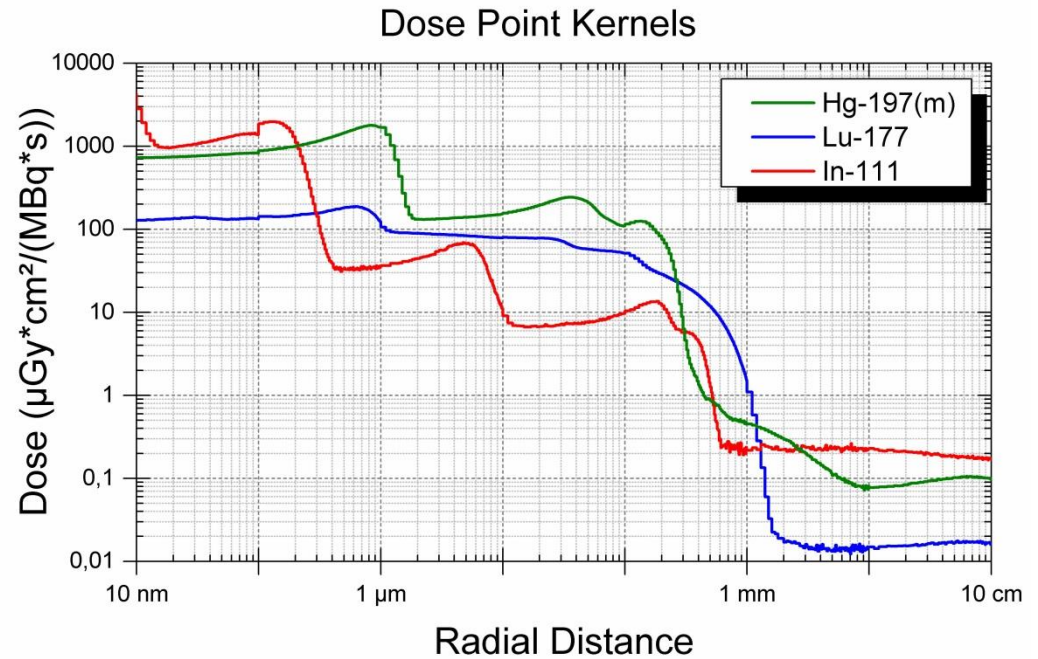


Fig. 2: Dose Point Kernels for different nuclides.

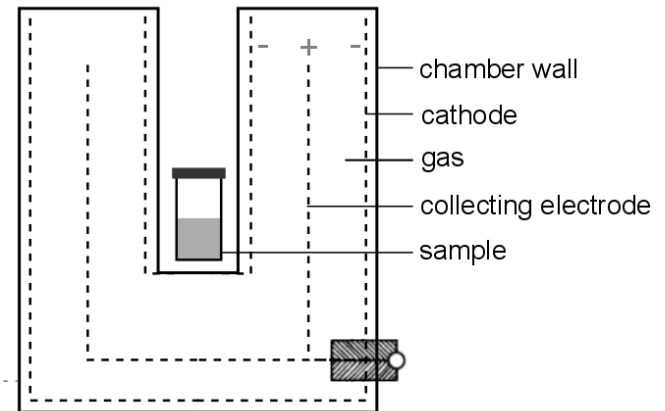
Motivation

Dose calibrator

- **ionization chamber** (*MED Isomed*)
- is used in clinical nuclear medicine laboratory to make measurements of radiopharmaceutical activities

function

- radiation interacts with atoms and molecules, resulting in ion pairs
- electrons move in the applied electrical field
- current produced is proportional to the amount of radioactivity and the energy of the photons
- different **current-activity conversion factors** for different isotopes and geometries



<http://www.springer.com/de/book/9783642811876>: Nuclear Medicine Part 1A
Radiopharmaceuticals Instrumentation Technology Radiation Protection

Motivation

Dose calibrator

- **ionization chamber**
- is used in clinical nuclear medicine laboratory to make measurements of radiopharmaceutical activities



function

- radiation interacts with atoms and molecules, resulting in ion pairs
- electric current is produced
- current is measured
- different isotopes and geometries

Usually: measurement of one single radionuclide



Hg-197(m): simultaneous measurement of two radionuclides

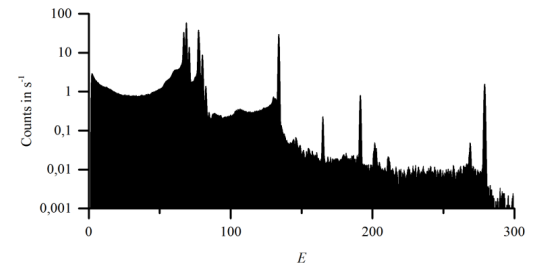
<http://www.springer.com/de/book/9783642811876>: Nuclear Medicine Part 1A
Radiopharmaceuticals Instrumentation Technology Radiation Protection

Method

Aim: measurement of Hg-197m and Hg-197 by a dose calibrator

Determination of radionuclide activity $A_{\text{Hg-197m}}$ and $A_{\text{Hg-197}}$ using gamma spectrometry (HPGe detector)

Full-energy peak efficiency calibration of the HPGe detector



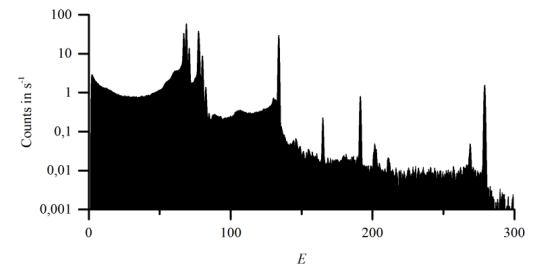
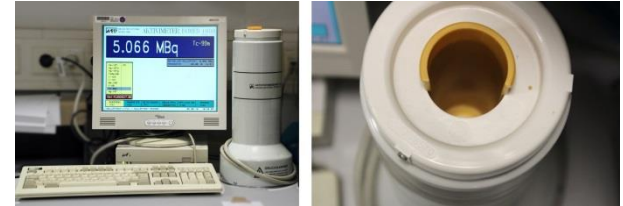
http://www.schott.com/pharmaceutical_packaging/german/products/vials/topline-options.html
<http://www.canberra.com/products/detectors/germanium-detectors.asp>

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<http://www.canberra.com/products/detectors/germanium-detectors.asp>

Efficiency calibration of the HPGe detector

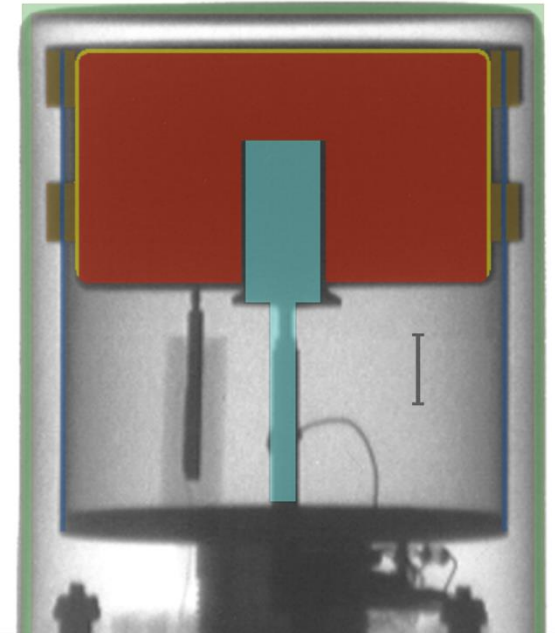
Experimental efficiency calibration

- calibration with standard point sources



Characterization with Monte Carlo simulations

- using Geant4
- efficiency values for point source and for vials



Efficiency calibration of the HPGe detector

Results

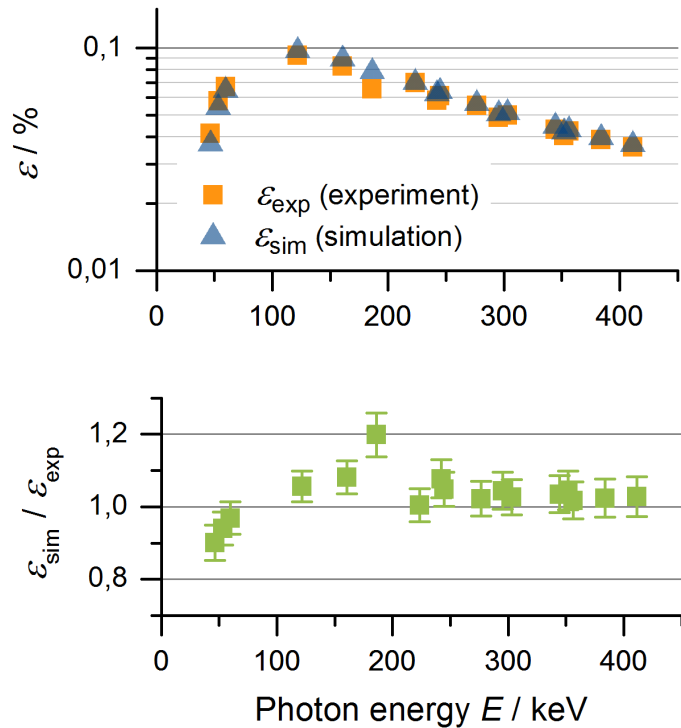


Fig. 3: Comparison between experimental and calculated full-energy peak efficiency ε for a source-to-detector distance of 40 cm

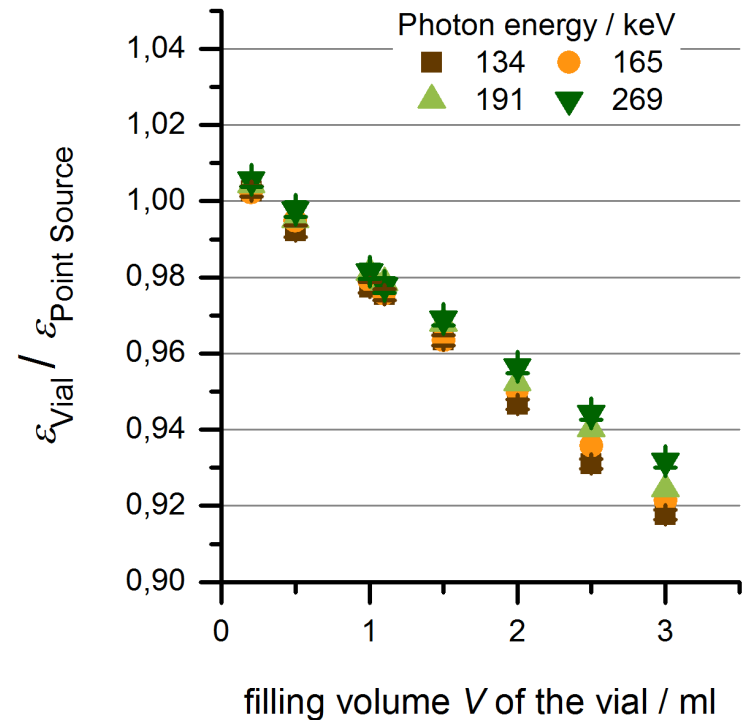


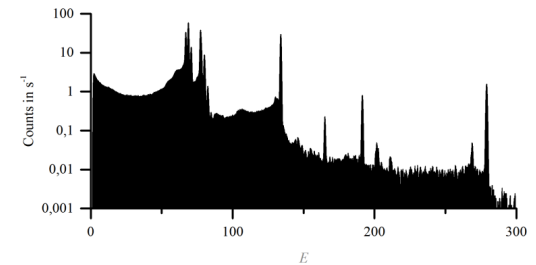
Fig. 4: Comparison between the efficiency for a point source and a vial with different filling volumes

Method

Aim: measurement of Hg-197m and Hg-197 by a dose calibrator



Determination of radionuclide activity $A_{\text{Hg-197m}}$ and $A_{\text{Hg-197}}$ using gamma spectrometry (HPGe detector)

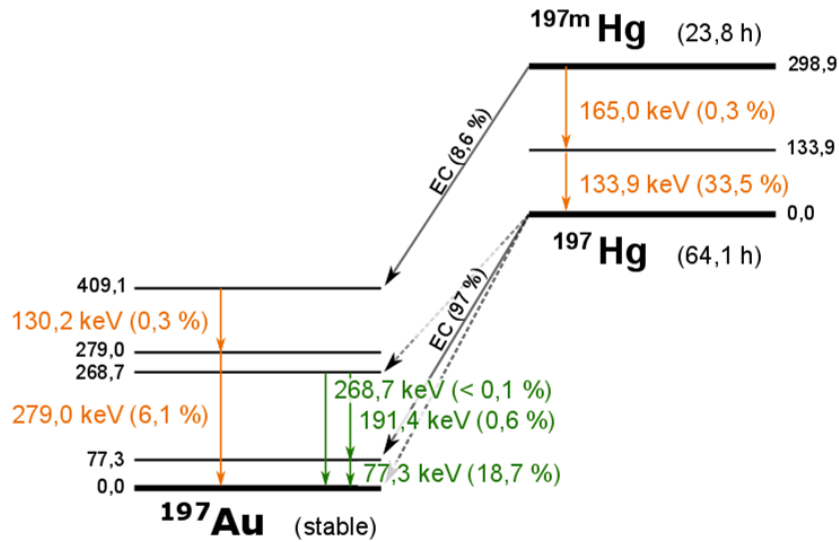


Full-energy peak efficiency calibration of the HPGe detector



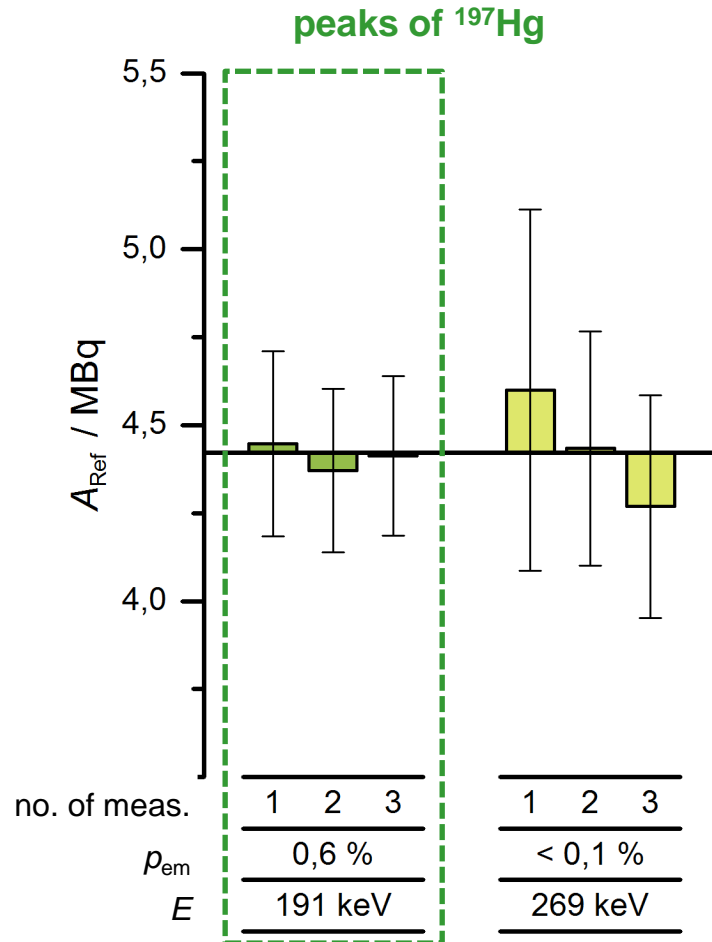
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Determination of radionuclide activity $A_{\text{Hg-197m}}$ and $A_{\text{Hg-197}}$

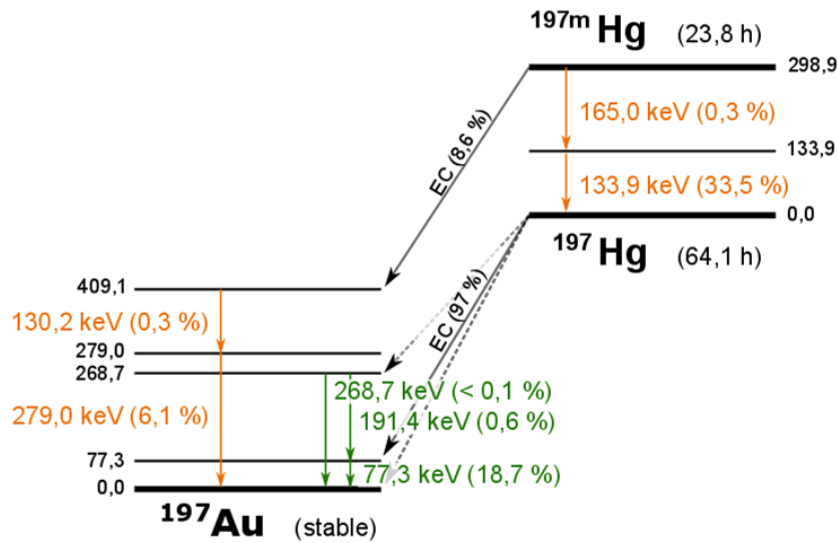


77 keV: low photon energy, close to the “knee” of $\epsilon(E)$, efficiency is not known precisely

269 keV: low photon emission probability

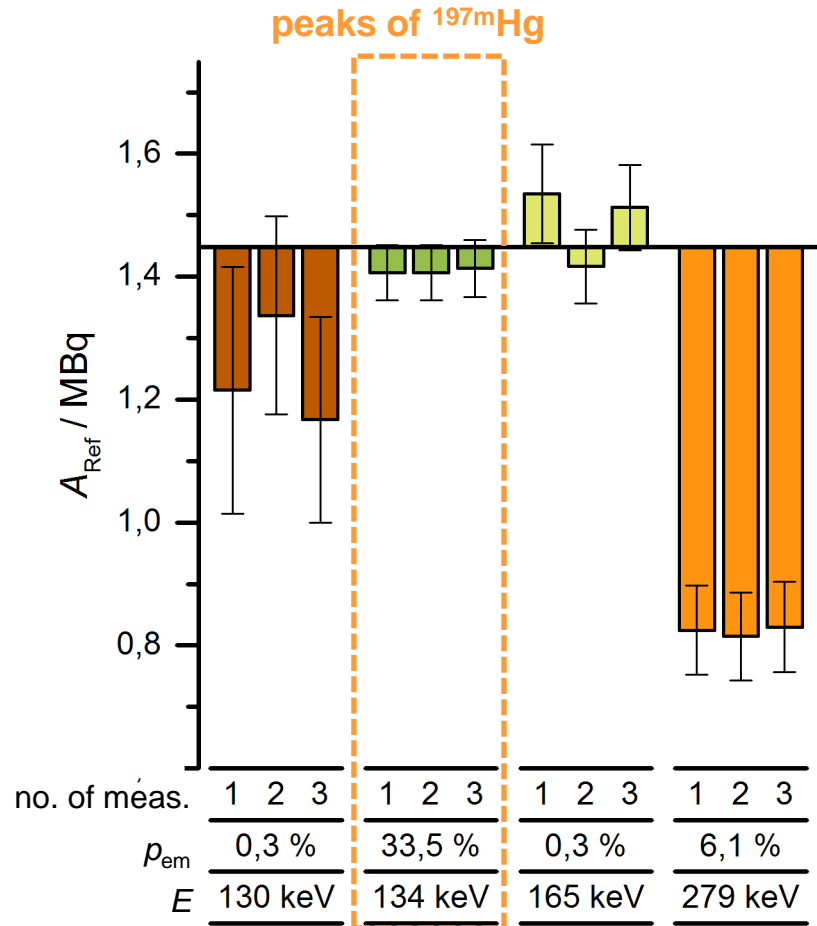


Determination of radionuclide activity $A_{\text{Hg-197m}}$ and $A_{\text{Hg-197}}$



134 keV and 165 keV: good agreement

130 keV and 279 keV: indicates a wrong photon emission probability

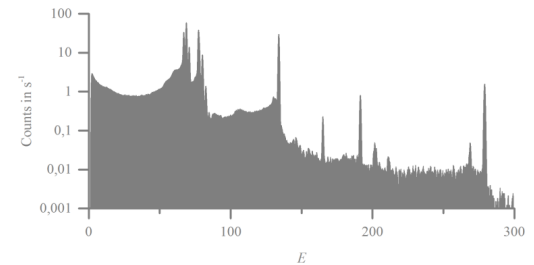


Method

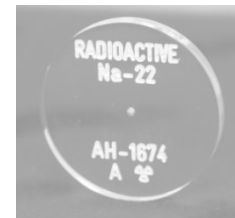
Aim: measurement of Hg-197m and Hg-197 by a dose calibrator



Determination of radionuclide activity $A_{\text{Hg-197m}}$ and $A_{\text{Hg-197}}$ using gamma spectrometry (HPGe detector) ✓



Full-energy peak efficiency calibration of the HPGe detector ✓



http://www.schott.com/pharmaceutical_packaging/german/products/vials/topline-options.html
<http://www.canberra.com/products/detectors/germanium-detectors.asp>

Measurement of Hg-197m and Hg-197 by a dose calibrator

Theoretical background

Response to a single radioisotope:

$$I_s = A \cdot \varepsilon$$

I_s ... detector reading
~ saturation current

$$\varepsilon = \sum_j p_{\beta j}(E_j) \cdot \varepsilon_{\beta j}(E_j) + \sum_i p_i(E_i) \cdot \varepsilon_i(E_i)$$

Response to a mixture of two radioisotopes

$$I_s = A_1 \cdot \varepsilon_1 + A_2 \cdot \varepsilon_2$$

A ... activity
 ε ... efficiency
 p ... emission probability

Measurement of Hg-197m and Hg-197 by a dose calibrator

Theoretical background

Response to a single radioisotope:

$$I_s = A \cdot \varepsilon$$

$$\varepsilon = \sum_j p_{\beta_j}(E_j) \cdot \varepsilon_{\beta_j}(E_j) + \sum_i p_i(E_i) \cdot \varepsilon_i(E_i)$$

Response to a mixture of two radioisotopes

$$I_s = A_1 \cdot \varepsilon_1 + A_2 \cdot \varepsilon_2$$

I_s ... detector reading
~ saturation current

A ... activity

ε ... efficiency

p ... emission probability

Calibration procedure

- ✓ A_1, A_2 are known (HPGe detector)
- ✗ ε_i have to be determined

→ At least two measurements
necessary
(different activity ratios)

Measurement of Hg-197m and Hg-197 by a dose calibrator

Theoretical background

Response to a single radioisotope:

$$I_s = A \cdot \varepsilon$$

$$\varepsilon = \sum_j p_{\beta j}(E_j) \cdot \varepsilon_{\beta j}(E_j) + \sum_i p_i(E_i) \cdot \varepsilon_i(E_i)$$

I_s ... saturation current
~ detector reading

A ... activity

ε ... efficiency

p ... emission probability

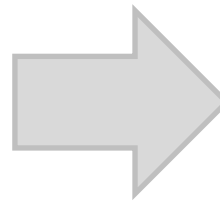
Response to a mixture of two radioisotopes

$$I_s = A_1 \cdot \varepsilon_1 + A_2 \cdot \varepsilon_2$$

Calibration procedure

- ✓ A_1, A_2 are known (HPGe detector)
- ✗ ε_i have to be determined

→ At least two measurements necessary
(different activity ratios)



Routine hospital practice

- ✓ ε_i are known
- ✗ A_1, A_2 have to be determined

→ two measurements necessary

$$I_s = A_1 \cdot \varepsilon_1 + A_2 \cdot \varepsilon_2$$

$$\tilde{I}_s = A_1 \cdot \tilde{\varepsilon}_1 + A_2 \cdot \tilde{\varepsilon}_2$$

(without / with copper shielding)

Measurement of Hg-197m and Hg-197 by a dose calibrator

Theoretical background: Selection of a shielding

without shielding $I_s = A_1 \cdot \varepsilon_1 + A_2 \cdot \varepsilon_2 \rightarrow A_1(A_2) = -\frac{\varepsilon_2}{\varepsilon_1} A_2 + \frac{I_s}{\varepsilon_1}$

with shielding $\tilde{I}_s = A_1 \cdot \tilde{\varepsilon}_1 + A_2 \cdot \tilde{\varepsilon}_2 \rightarrow A_1(A_2) = -\frac{\tilde{\varepsilon}_2}{\tilde{\varepsilon}_1} A_2 + \frac{\tilde{I}_s}{\tilde{\varepsilon}_1}$

- two lines with different slopes

- aim: maximize angle of intersection, i.e. $\frac{\varepsilon_2}{\varepsilon_1} \neq \frac{\tilde{\varepsilon}_2}{\tilde{\varepsilon}_1}$

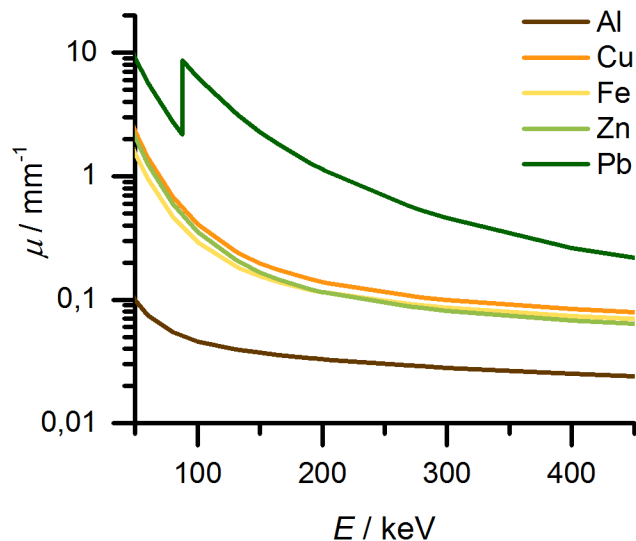


Fig. 5: Linear attenuation coefficient for photons in different materials as a function of photon energy

→ Use copper for shielding

Measurement of Hg-197m and Hg-197 by a dose calibrator

Determination of radionuclide efficiencies ε_i

1. preparation of a **serial dilution** in order to cover a range of activities with different ratios of $A_{\text{Hg-197m}}$ to $A_{\text{Hg-197}}$



2. **determination of $A_{\text{Hg-197m}}$ and $A_{\text{Hg-197}}$** of samples using HPGe detector

3. **multiple measures with dose calibrator** at different times, with and without shielding



4. determination of ε_i by **nonlinear curve fitting of all dose calibrator readings**

Measurement of Hg-197m and Hg-197 by a dose calibrator

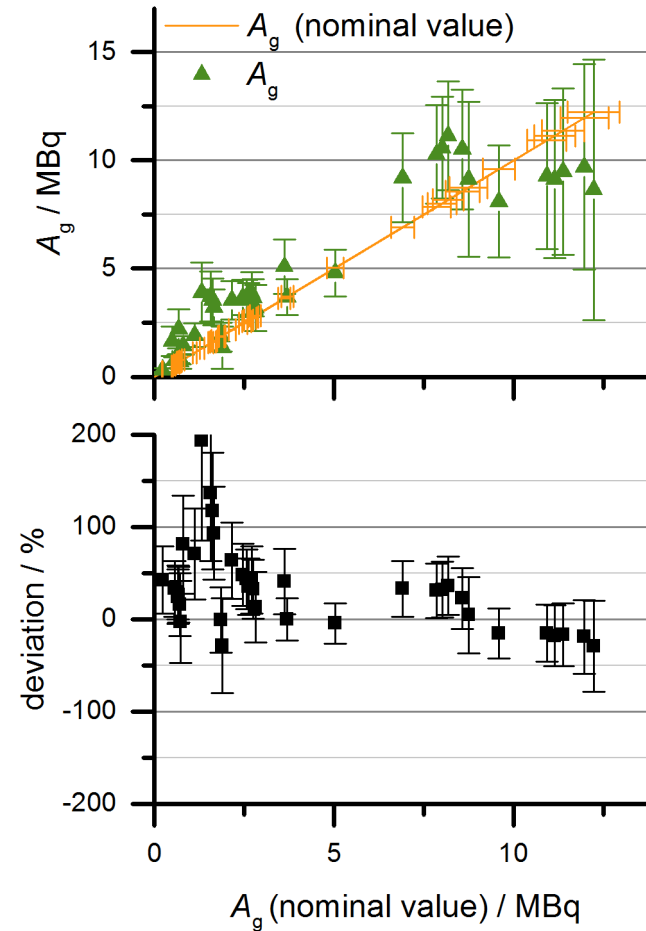
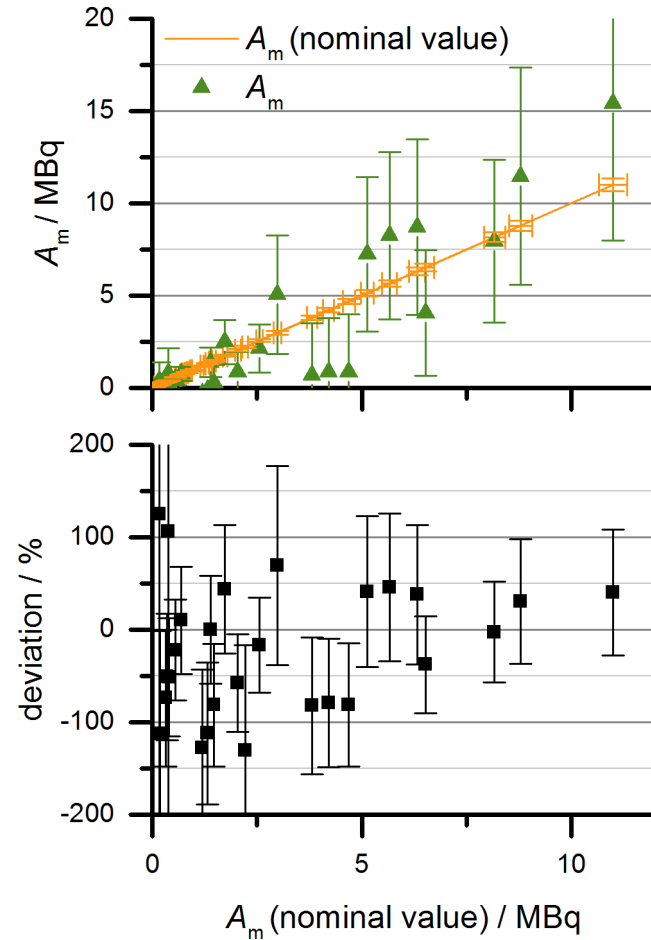
Determination of radionuclide efficiencies ε_i

shielding	ε_m	$\tilde{\varepsilon}_m$		ε_g	$\tilde{\varepsilon}_g$	
	no	1 mm	2 mm	no	1 mm	2 mm
value	$9,9 \pm 0,9$	$6,87 \pm 0,17$	$5,3 \pm 0,5$	$14,6 \pm 0,5$	$8,38 \pm 0,11$	$6,36 \pm 0,29$
relative uncertainty	8,8 %	2,4 %	8,8 %	3,5 %	1,3 %	4,5 %

Measurement of Hg-197m and Hg-197 by a dose calibrator

Calculated activities compared with nominal values

shielding:
1 mm



Measurement of Hg-197m and Hg-197 by a dose calibrator

Consideration of uncertainties

$$\left. \begin{aligned} I &= A_m \cdot \varepsilon_m + A_g \cdot \varepsilon_g \\ \tilde{I} &= A_m \cdot \tilde{\varepsilon}_m + A_g \cdot \tilde{\varepsilon}_g \end{aligned} \right\} \begin{aligned} A_m &= \frac{I}{\varepsilon_m} - \frac{\frac{\varepsilon_g}{\varepsilon_m} \left(\tilde{I} - \frac{\tilde{\varepsilon}_m}{\varepsilon_m} I \right)}{\tilde{\varepsilon}_g - \frac{\tilde{\varepsilon}_m}{\varepsilon_m} \varepsilon_g} \\ A_g &= \frac{\tilde{I} - \frac{\tilde{\varepsilon}_m}{\varepsilon_m} I}{\tilde{\varepsilon}_g - \frac{\tilde{\varepsilon}_m}{\varepsilon_m} \varepsilon_g} \end{aligned}$$

elements of uncertainty: $\varepsilon_m, \varepsilon_g, \tilde{\varepsilon}_m, \tilde{\varepsilon}_g, I, \tilde{I}$

Example:

quantity	ε_m	$\tilde{\varepsilon}_m$	ε_g	$\tilde{\varepsilon}_g$	I	\tilde{I}	A_m	A_g
relative uncertainty / %	8,8	2,4	3,5	1,3	0,05 ... 0,4	0,1 ... 1,2	<u>48 ... >100</u>	<u>22 ... 71</u>

Conclusions

- **HPGe detector:**
 - $A_{\text{Hg-197}}$ and $A_{\text{Hg-197m}}$ with relative uncertainties between 3,2 and 5,0 % determined
- **Dose calibrator:**
 - Efficiencies for Hg-197 and Hg-197m determined
 - Good agreement between calculated activities and nominal values within the scope of their uncertainties
 - Consideration of the uncertainties is a very important point

Limitations:

- Great uncertainties of calculated activities
- Not applicable in clinical routine at the moment

Conclusions

Alternative method:

- Determination of $A_{\text{Hg-197}}$, $A_{\text{Hg-197m}}$ using HPGe detector
- Calculation of $A_{\text{Hg-197}}(t)$, $A_{\text{Hg-197m}}(t)$ using equations for radioactive decay chain

Limitations:

- More time-consuming than measurements with a dose calibrator
- Requires HPGe detector
- Uncertainty of activity ratio, photon emission probability and half life
 - great uncertainties in calculated activities for later times
 - should only be used for short periods of time

Thank you very much for your attention!

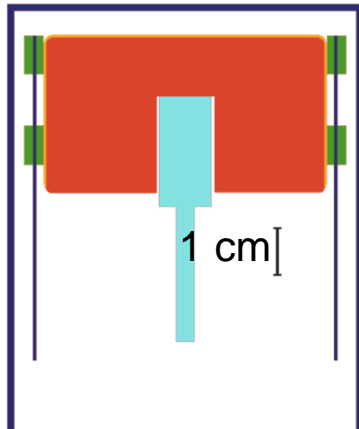
Contact: Robert.Freudenberg@uniklinikum-dresden.de

Maria.Vogel@uniklinikum-dresden.de

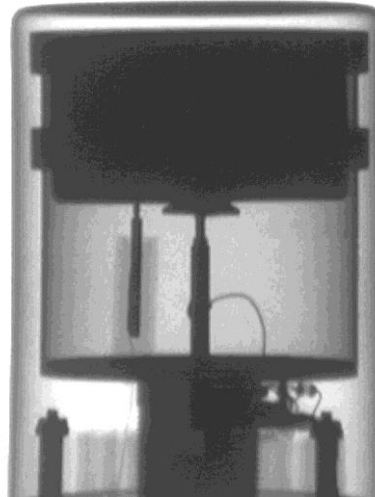
Efficiency calibration of the HPGe detector

Characterization with Monte Carlo simulations

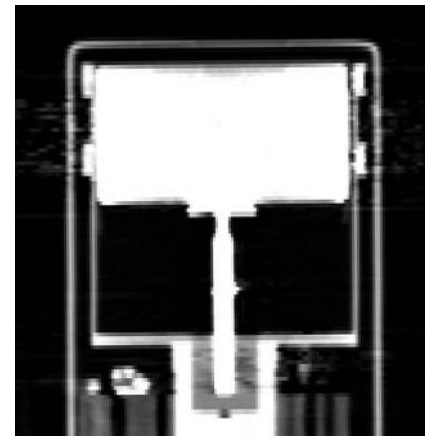
- using the Geant4 toolkit
- geometry was initially modeled using technical dimensions supplied by the manufacturer
- optimization:
 - information from X-ray and CT images
 - comparison between experimental and calculated full-energy peak efficiency for different detector parameter set-ups at the reference geometry (point sources)



Geant4 detector model

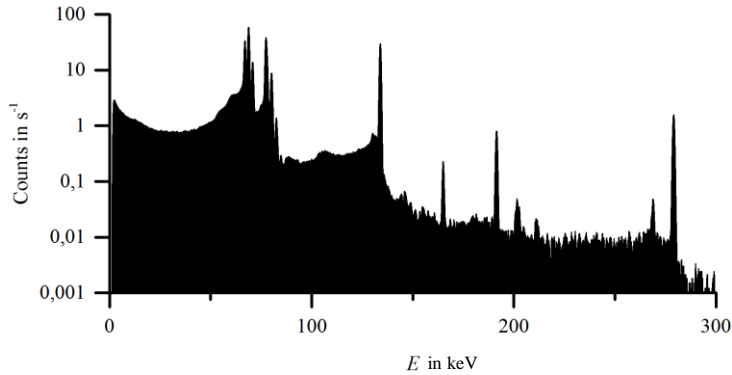


X-ray scan

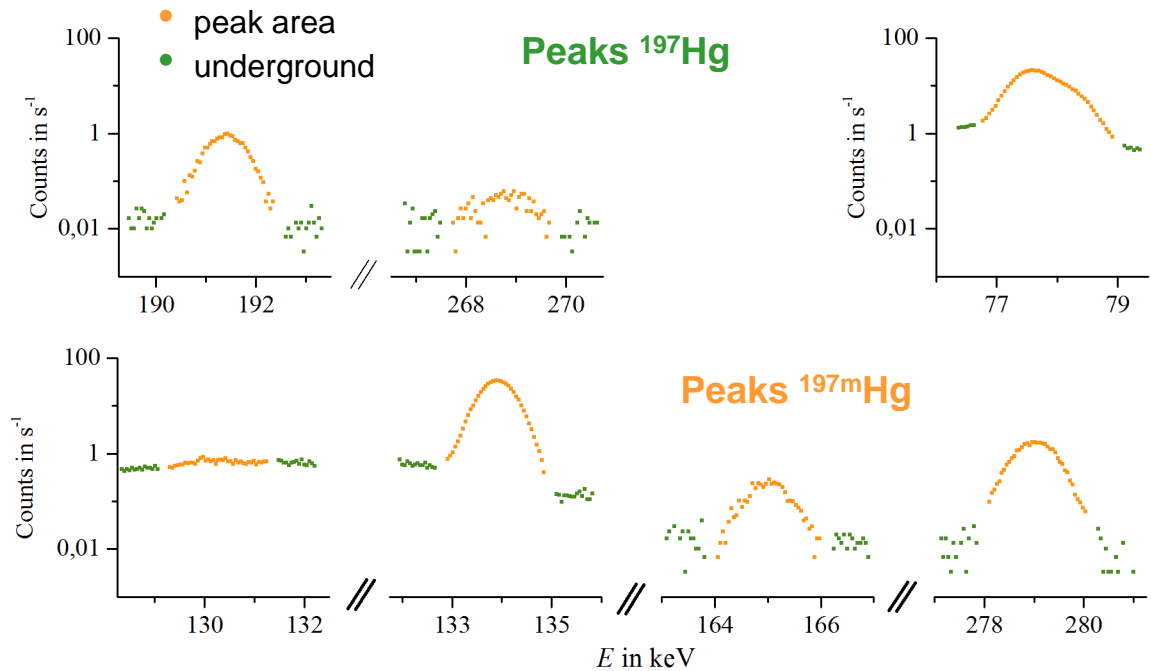


CT scan

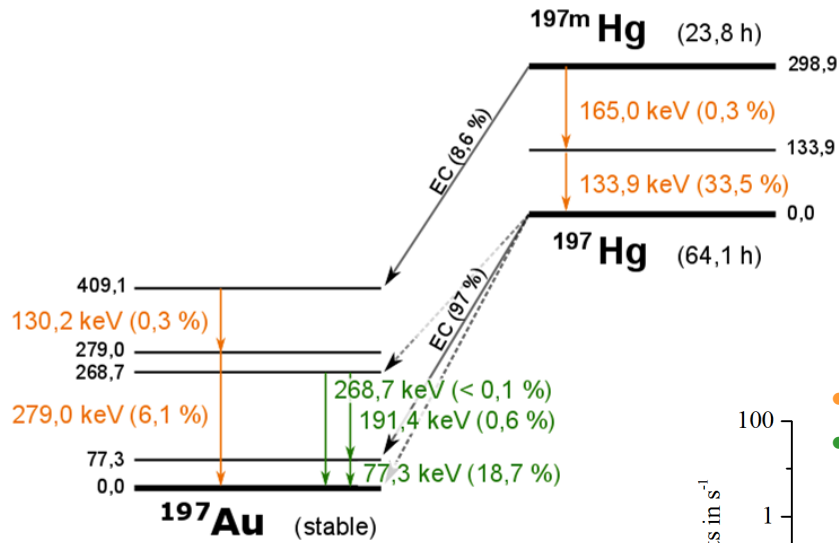
Determination of radionuclide activity $A_{\text{Hg-197m}}$ and $A_{\text{Hg-197}}$



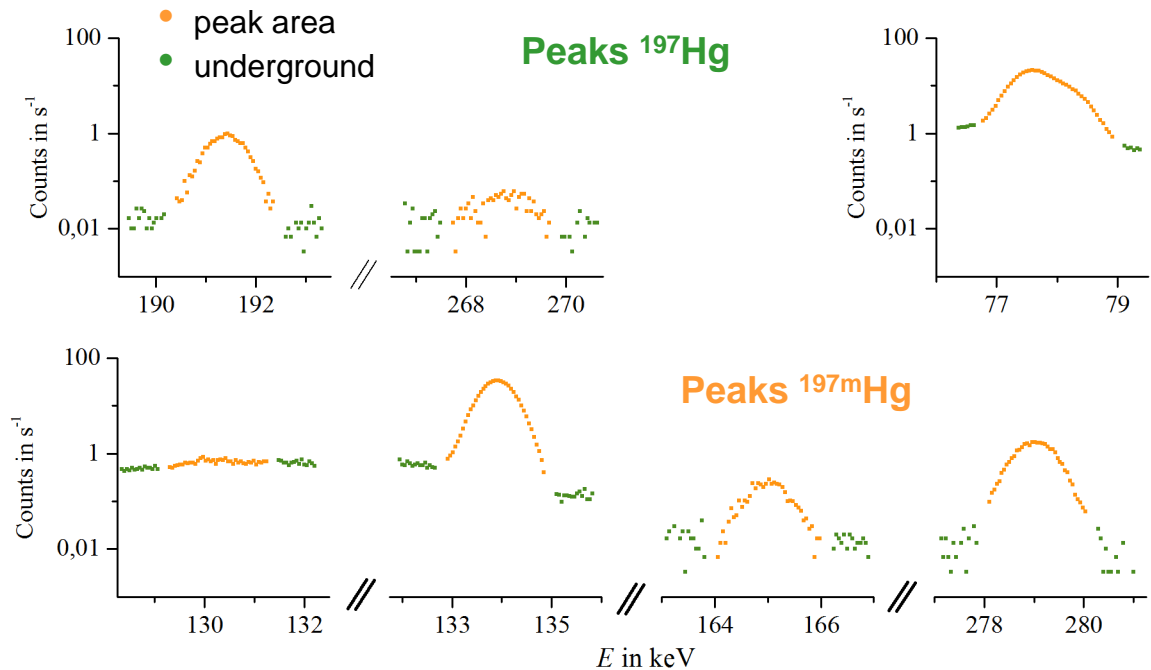
detector efficiency ε :
$$\varepsilon = \frac{N_{\text{VEP}}}{A_0 t p_{\text{em}}}$$



Determination of radionuclide activity $A_{\text{Hg-197m}}$ and $A_{\text{Hg-197}}$



detector efficiency ε :
$$\varepsilon = \frac{N_{\text{VEP}}}{A_0 t p_{\text{em}}}$$



Measurement of Hg-197 and Hg-197m by a dose calibrator

Quality control

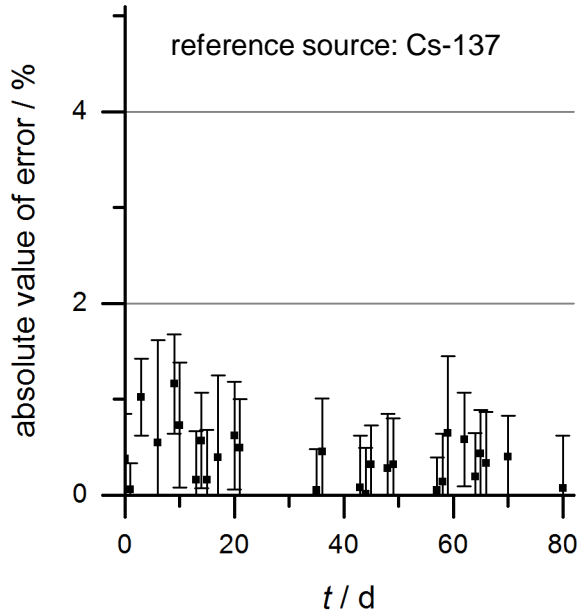
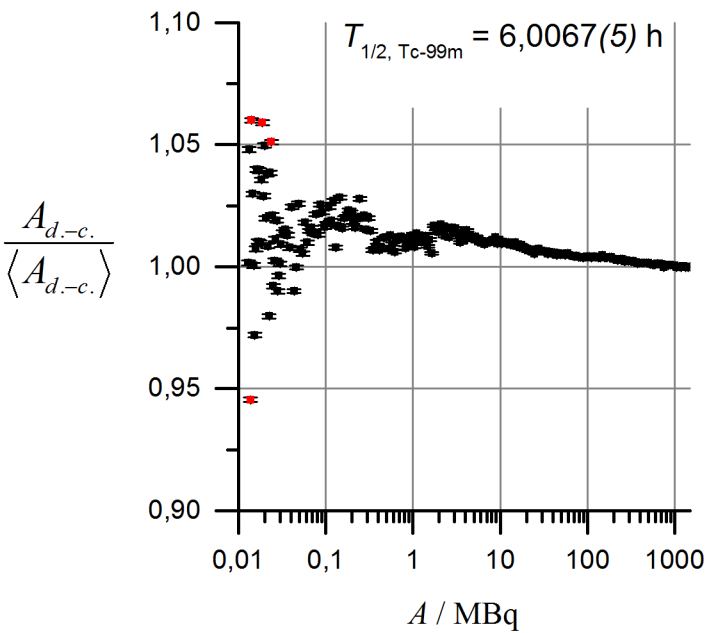
- dose calibrators can remain stable over several years
- they are critical to the work of a nuclear medicine department



Test	Constancy	Activity linearity
Recommended Frequency	Daily	Half-yearly
	Reading of the activity of a long-lived reference source (usually Cs-137)	Measure a short-lived source (Tc-99m) at several time points (from 1 MBq to 1 GBq or more)
Acceptable error <math>< \pm 5 \%</math>		

Measurement of Hg-197 and Hg-197m by a dose calibrator

Quality control

Test	Constancy	Activity linearity
	 <p>reference source: Cs-137</p> <p>absolute value of error / %</p> <p>t / d</p>	 <p>$T_{1/2, Tc-99m} = 6,0067(5) \text{ h}$</p> <p>$\frac{A_{d-c.}}{\langle A_{d-c.} \rangle}$</p> <p>A / MBq</p>
	<p>Fig. X: Results of the constancy test.</p>	<p>Fig. X: Results of the activity linearity test using a Tc-99m source and decay-corrected activities $A_{d-c.}$</p>

Measurement of Hg-197 and Hg-197m by a dose calibrator

Determination of radionuclide efficiencies ε_i

1. preparation of a **serial dilution** in order to cover a range of activities with different ratios of $A_{\text{Hg-197m}}$ to $A_{\text{Hg-197}}$



2. **determination of $A_{\text{Hg-197m}}$ and $A_{\text{Hg-197}}$** of samples using HPGe detector



3. **multiple measures with dose calibrator** at different times, with and without shielding



4. multiple **controls of $A_{\text{Hg-197m}}$ and $A_{\text{Hg-197}}$** using HPGe detector



Method a)

5. determination of ε_i by **nonlinear curve fitting of all dose calibrator readings**

Measurement of Hg-197 and Hg-197m by a dose calibrator

Determination of radionuclide efficiencies ϵ_i

1. preparation of a **serial dilution** in order to cover a range of activities with different ratios of $A_{\text{Hg-197m}}$ to $A_{\text{Hg-197}}$

2. **determination of $A_{\text{Hg-197m}}$ and $A_{\text{Hg-197}}$** of samples using HPGe detector

3. **multiple measures with dose calibrator** at different times, with and without shielding

4. multiple **controls of $A_{\text{Hg-197m}}$ and $A_{\text{Hg-197}}$** using HPGe detector

Method a)

5. determination of ϵ_i by **nonlinear curve fitting of all dose calibrator readings**

Method b)

5. **determination of $\epsilon_{\text{Hg-197}} == \epsilon_g$** by analysis of dose calibrator readings of decayed samples ($A_{\text{Hg-197m}} \ll A_{\text{Hg-197}}$)
6. **determination of $\epsilon_{\text{Hg-197m}} == \epsilon_m$** by analysis of other dose calibrator readings

Measurement of Hg-197 and Hg-197m by a dose calibrator

Determination of radionuclide efficiencies ϵ_i

Method a)

5. determination of ϵ_i by **nonlinear curve fitting of all dose calibrator readings**

Method b)

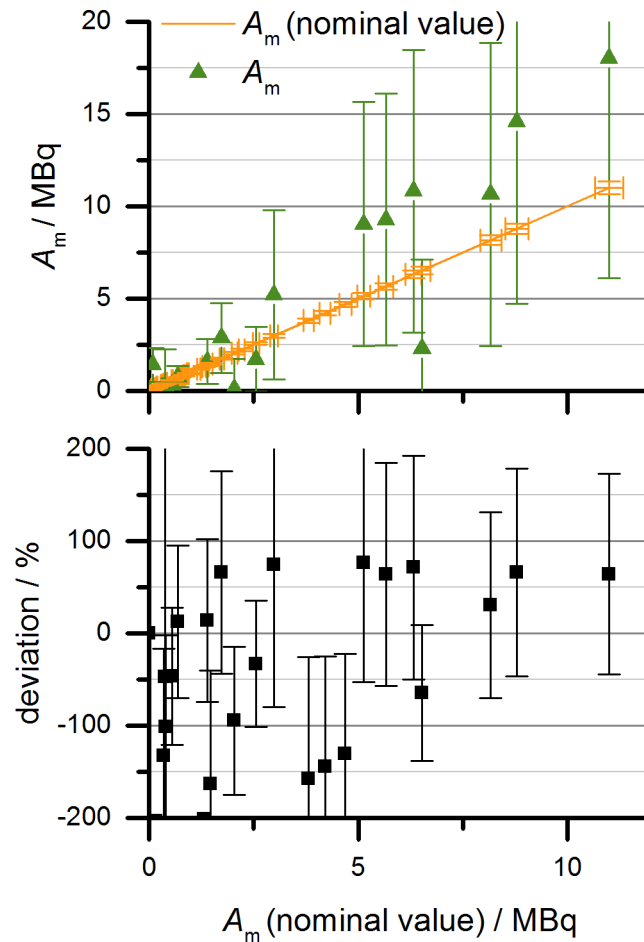
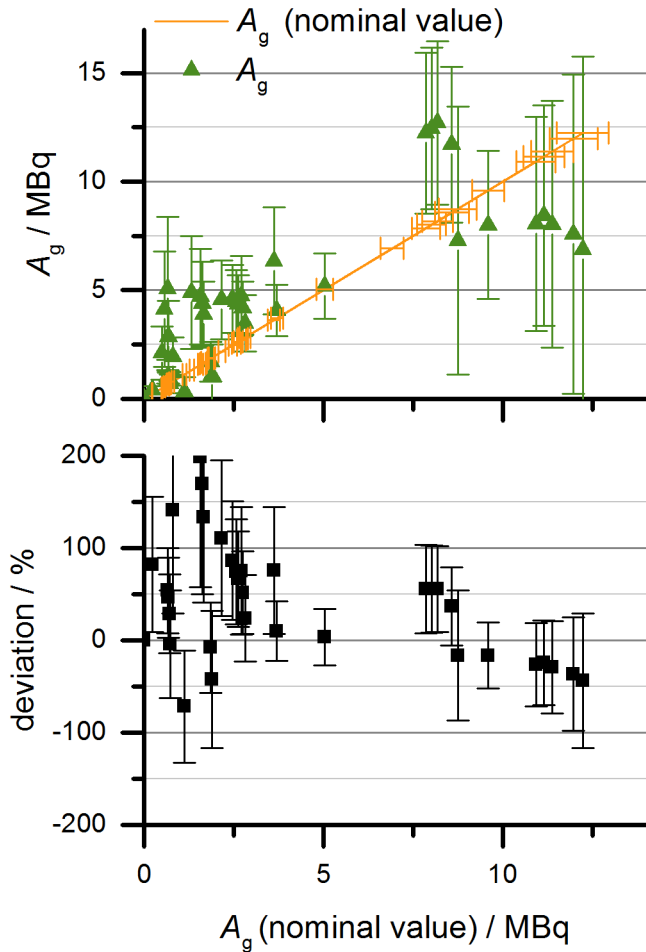
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6. **determination of $\epsilon_{\text{Hg-197m}} == \epsilon_m$** by analysis of other dose calibrator readings

	shielding	ϵ_m			ϵ_g		
		no	1 mm	2 mm	no	1 mm	2 mm
Method a)	value	$9,9 \pm 0,9$	$6,87 \pm 0,17$	$5,3 \pm 0,5$	$14,6 \pm 0,5$	$8,38 \pm 0,11$	$6,36 \pm 0,29$
	rel. unc. / %	8,8	2,4	8,8	3,5	1,3	4,5
Method b)	value	$9,1 \pm 0,4$	$6,4 \pm 0,3$	-	$15,28 \pm 0,28$	$8,64 \pm 0,22$	-
	rel. unc. / %	4,4	4,7	-	1,8	2,5	-

Measurement of Hg-197 and Hg-197m by a dose calibrator

Calculated activities compared with nominal values

Method a),
shielding:
2 mm



Measurement of Hg-197 and Hg-197m by a dose calibrator

Calculated activities compared with nominal values

Method b)

