# Reasoning in Description Logic Ontologies for Privacy Management

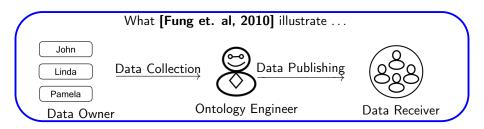
Adrian Nuradiansyah

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September 27, 2019



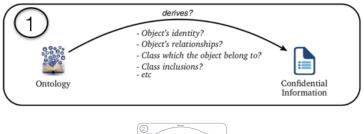
### Data Collection and Data Publishing for Ontologies

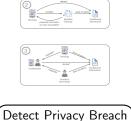


In the context of Description Logic Ontologies, [Grau, 2010] concerns ...

- A rise in the number of ontologies integrated in mainstream applications, e.g., medical systems
- Possible unauthorized disclosures of medical information may occur
- Designing privacy-preserving systems is being a critical requirement

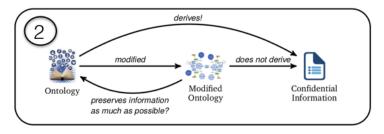
#### What Should the Engineer Do Before Publishing?





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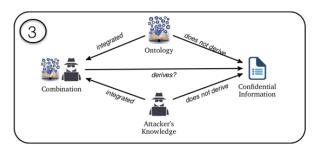




Detect Privacy Breach Ontology Repair

#### What Should the Engineer Do Before Publishing?









- Confidential information ⇒ property of individuals
- Membership of individuals (tuple of individuals) in the answers to certain queries (e.g., [Calvanesse et. al., 2008], [Stouppa & Studer, 2009], [Tao et.al., 2010] )



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Focus on Identity? What is "identity"?



- Finding justifications why the (unwanted) consequences can be derived (e.g., [Schlobach, 2003], [Parsia et. al., 2007], [Baader et. al., 2008])
- Remove axioms that are responsible for the entailment (e.g., [Kalyanpur et. al., 2006])



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Do these approaches also remove useful consequences?

Can we do it more "gentle"?



- Learning type of attackers' background knowledge
- Investigating attribute linkage, table linkage, etc thoroughly in e.g., [Fung et. al., 2010]
- Introducing the notion of policy-compliance and policy-safety in the context of RDF graphs/Linked Data in e.g., [Grau & Kostylev, 2016]



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[Is such setting already considered in DL ontologies?]

#### Problem Descriptions

Detecting Privacy Breach

The Identity Problem and its Variants in Description Logic Ontologies

Ontology Repair

Repairing Description Logic Ontologies via Axiom Weakening

Avoiding Linkage Attacks

Privacy-Preserving Ontology Publishing

# Description Logics (DLs)

The logical underpinning of Web Ontology Language (OWL)

Decidable fragments of First Order Logics

Representing the conceptual knowledge of an application domain in a well-understood way.

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Representing the conceptual knowledge of an application domain in a well-understood way.

Non-German people who work at an IT Department whose all locations are either in Germany or in Austria



 $\neg$  German  $\sqcap \exists$  worksAt.(ITDept  $\sqcap \forall$  located.(Germany  $\sqcup$  Austria))

Name	Syntax	Example
Тор	Т	tautology
Concept Name	А	Germany
Conjunction	$C \sqcap D$	German □ Female
Disjunction	$C \sqcup D$	Germany ⊔ Austria
Existential Restriction	∃r.C	German □ ∃worksAt.ITDept
Universal Restriction	∀r.C	$ITDept \sqcap \forall located. Germany$
Negation	$\neg C$	¬German
(One of) Nominal	$\{a_1,\ldots,a_n\}$	{LINDA, JOHN, JIM}

Name	Syntax	Example
Тор	Т	tautology
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ALC

- Closed under Boolean operators - Intractable

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 $\mathcal{EL}$ 

inexpressive, but reasoning is in PTime

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 $\mathcal{FL}_0$ 

The dual of  $\mathcal{EL}$ 

Name	Syntax	Example
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Disjunction	$C \sqcup D$	Germany ⊔ Austria
Existential	∃r.C	German □ ∃worksAt.ITDept
Restriction		,
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 $\mathcal{FLE}$ 

Combination of  $\mathcal{EL}$  and  $\mathcal{FL}_0$ 

### DL Ontologies

A DL ontology  $\mathfrak O$  consists of an ABox  $\mathcal A$  and a TBox  $\mathcal T \Longleftrightarrow \mathfrak O = (\mathcal A, \mathcal T)$ 

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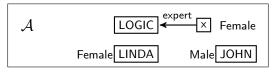
An ABox A: **knowledge about individuals** (instance relationships C(a) and individual relationships r(a,b))



A TBox  $\mathcal{T}$ : inclusion relationships/constraints between concepts  $C \sqsubseteq D$  (General Concept Inclusions (GCIs))

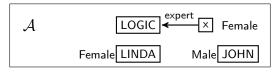
 $\mathcal{T}$   $\exists$ expert. $\{LOGIC\} \sqsubseteq VerTeam$   $Female \sqsubseteq \neg Male$ 

### What can I Infer from an Ontology?



```
\mathcal{T} \exists expert.\{LOGIC\} \sqsubseteq VerTeam Female \sqsubseteq \neg Male VerTeam \equiv \{LINDA, JOHN\}
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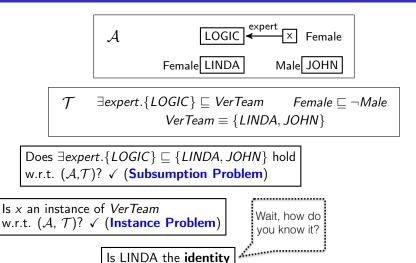


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```
Does \exists expert.\{LOGIC\} \sqsubseteq \{LINDA, JOHN\} \text{ hold } w.r.t. (A,T)? \checkmark (Subsumption Problem)
```

```
Is x an instance of VerTeam w.r.t. (A, T)? \checkmark (Instance Problem)
```

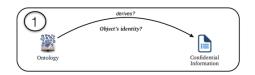
# What can I Infer from an Ontology?



how do we call this

of anonymous x?  $\checkmark$ 

# Problem 1: Is My Identity Safe?







Identity Problem ( $\mathfrak{O} \models x = a$ ) [DL 2017], [JIST 2017]

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- DLs with equality power: nominals, number restrictions, and functional dependencies.

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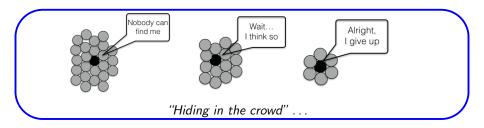


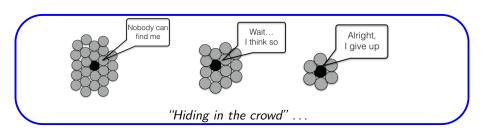


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- ullet Not all DLs are able to derive equalities between individuals, e.g.  $\mathcal{ALC}$ .
- DLs with equality power: nominals, number restrictions, and functional dependencies.
- **Identity to Instance**: Given two individuals x, a, and an ontology  $\mathfrak O$  formulated in a DL with equality power, it holds

 $\mathfrak{O} \models x \doteq a \text{ iff } (\mathfrak{O} \cup \{Q(x)\}) \models Q(a), \text{ where } Q \text{ is a fresh concept name}$ 

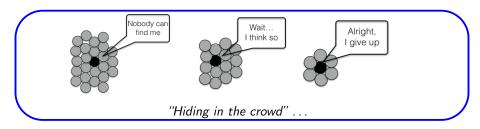




#### *k*-Hiding

The anonymous individual x is **not** k**-hidden** w.r.t.  $\mathfrak O$  iff there are known individuals  $a_1, \ldots, a_{k-1}$  such that

x belongs to  $\{a_1,\ldots,a_{k-1}\}$  w.r.t.  $\mathfrak O$ 



#### k-Hiding

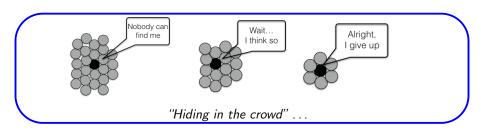
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#### How to solve it

- Reduce it to the instance problem for all DLs with equality power
- Reduce it to the identity problem for some convex DLs with equality power

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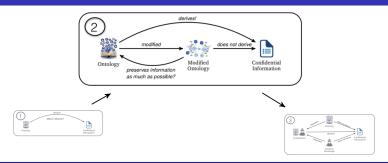
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If (variants) of the identity problem can be reduced to classical reasoning problems in DLs, then now let's consider **more general types of confidential axioms** (e.g., instance relationships, subsumptions, CQs, etc).

#### Problem 2: How to Protect the Confidential Information?

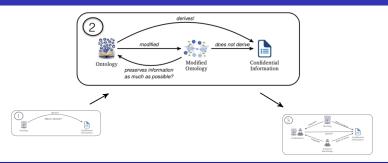


#### Ontology Repair ([KR 2018], [DL 2018])

- $\mathfrak{O} = \mathfrak{O}_s \cup \mathfrak{O}_r$ , where  $\mathfrak{O}_s$  is a static ontology and  $\mathfrak{O}_r$  is a refutable ontology.
- Let  $Con(\mathfrak{O}) := \{ \alpha \mid \mathfrak{O} \models \alpha \}$  be the set of all consequences of  $\mathfrak{O}$ .

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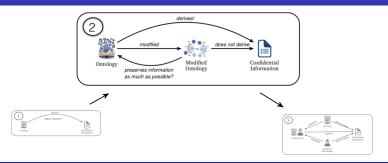
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$$Con(\mathfrak{O}_s \cup \mathfrak{O}') \subseteq Con(\mathfrak{O}) \setminus \{\alpha\}$$

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• Optimal repair  $\mathfrak{D}'$  of  $\mathfrak{D}$  w.r.t.  $\alpha$ : No Repair  $\mathfrak{D}''$  of  $\mathfrak{D}$  w.r.t.  $\alpha$  such that  $Con(\mathfrak{D}' \cup \mathfrak{D}_s) \subset Con(\mathfrak{D}'' \cup \mathfrak{D}_s)$ .

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Optimal Repairs need not exist in general!

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A maximum subset  $\mathfrak{O}'$  of  $\mathfrak{O}_r$  such that  $\mathfrak{O}_s \cup \mathfrak{O}' \not\models \alpha$ 

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- Optimal classical repairs always exist → Justification and Hitting Set (Reiter, 1987)
- Let  $\mathfrak{D}\models\alpha$ . A justification J of  $\mathfrak{D}$  w.r.t.  $\alpha$  is a minimal subset of  $\mathfrak{D}_r$  s.t.  $\mathfrak{D}_s\cup J\models\alpha$ .
- Let  $J_1, \ldots, J_k$  be the justifications of  $\mathfrak O$  w.r.t.  $\alpha$ . A **hitting set**  $\mathcal H$  of these justifications is a set of axioms such that  $\mathcal H \cap J_i \neq \emptyset$
- A hitting set  $\mathcal{H}_{min}$  is minimal if there is no  $\mathcal{H}'$  of  $J_1, \ldots, J_k$  such that  $\mathcal{H}' \subset \mathcal{H}_{min}$ .
- $\mathfrak{D}' := \mathfrak{D}_r \setminus \mathcal{H}_{min}$  is an optimal classical repair of  $\mathfrak{D}$  w.r.t.  $\alpha$  such that

$$\mathfrak{O}_{\mathfrak{s}} \cup \mathfrak{O}' \not\models \alpha$$



Obtaining Classical Repairs  $\rightarrow$  removing axioms from  $\mathfrak{O}$ .

Instead, we want to weaken axioms in  $\mathcal{H} \Rightarrow$  Gentle Repair!

Given axioms  $\beta, \gamma$ , an axiom  $\gamma$  is weaker than  $\beta$  if  $Con(\{\gamma\}) \subset Con(\{\beta\})$ 

#### Illustration

```
\mathfrak{O}_s := \{\exists receives.(Gift \sqcap Deluxe) \sqsubseteq \exists gets.Bribe\}
\mathfrak{O}_r := \{IndonesianPolitician \sqsubseteq \exists receives.(Gift \sqcap Deluxe)\}
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• Every Indonesian politician is bribed w.r.t.  $\mathfrak{O}_s \cup \mathfrak{O}_r$ .







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- More gentle: Weaken β to IndonesianPolitician 
   □ ∃receives. Gift □ ∃receives. Deluxe







### How to Make it Gentle?

#### Gentle Repair Algorithm: [BaKrNuPe, KR 2018]

- ullet Take all justifications and one minimal hitting set  ${\cal H}_{\it min}$
- For each  $\beta \in \mathcal{H}_{min}$  and all  $J_1, \ldots, J_k$  containing  $\beta$ , replace  $\beta$  with exactly one  $\gamma$ , where  $\gamma$  is weaker than  $\beta$  such that

$$\mathfrak{O}_s \cup (J_i \setminus \{\beta\}) \cup \{\gamma\} \not\models \alpha \text{ for } i = 1, \dots, k.$$
 (1)

 $\gamma$  always exists.

- Construct  $\mathfrak{O}'$  obtained from  $\mathfrak{O}_r$  by replacing each  $\beta \in \mathcal{H}_{min}$  with an appropriate weaker  $\gamma$  satisfying (1).
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### Obtaining Gentle Repairs needs Iterations

- Using the algorithm above,  $\alpha$  still can be a consequence of  $\mathfrak{O}_s \cup \mathfrak{O}'$ .
- Solution: Just iterate Gentle Repair Algorithm until  $\mathfrak{O}_s \cup \mathfrak{O}' \not\models \alpha$ .
- The iterative algorithm yields an exponential upper bound on the number of iterations.

# Weakening Relations

To obtain better bounds on the number of iterations, introduce weakening relations on axioms.

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#### Weakening Relation

The binary relation ≻ on axioms is

- a weakening relation if  $\beta \succ \gamma$  implies that  $\gamma$  is weaker than  $\beta$ ;
- well-founded if there is no infinite  $\succ$ -chain  $\beta_1 \succ \beta_2 \succ \beta_3 \succ ...$ ;
- complete if for any  $\beta$  that is not a tautology, there is a tautology  $\gamma$  s.t.  $\beta \succ \gamma$ .
- linear (polynomial) if for every axiom  $\beta$ , the length of the longest chain  $\succ$ -generated from  $\beta$  is linearly (polynomially) bounded by the size of  $\beta$ ;

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Weakening relations making larger steps may decrease the number of iterations



Weakening relations making smaller steps may make the repair more gentle

# Maximally Strong Weakening Axioms

Replace  $\beta$  with exactly one weaker  $\gamma$  s.t.

$$\mathfrak{D}_{s} \cup (J_{i} \setminus \{\beta\}) \cup \{\gamma\} \not\models \alpha \text{ for } i = 1, \dots, k$$

If  $\gamma$  is a tautology, then it is the same as classical repair.

To make this repair as gentle as possible,  $\gamma$  should be maximally strong

$$\mathfrak{O}_{s} \cup (J_{i} \setminus \{\beta\}) \cup \{\gamma\} \not\models \alpha$$
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Do they always exists?

How to compute them?

# Weakening Relations in $\mathcal{EL}$

Focus on GCIs and generalize the right-hand side of GCIs.

#### A Weakening Relation ≻<sup>sub</sup>

$$C \sqsubseteq D \succ^{sub} C' \sqsubseteq D'$$
 if  $C' = C$ ,  $D \sqsubset D'$ , and  $\{C' \sqsubseteq D'\} \not\models C \sqsubseteq D$ .

 $D \sqsubseteq^{\mathit{syn}} D' \Rightarrow \mathsf{removing} \ \mathsf{occurrences} \ \mathsf{of} \ \mathsf{subconcepts} \ \mathsf{of} \ D.$ 

#### A Weakening Relation ≻<sup>syn</sup>

$$C \sqsubseteq D \succ^{syn} C' \sqsubseteq D'$$
 if  $C' = C$  and  $D \sqsubseteq^{syn} D'$ , and  $\{C' \sqsubseteq D'\} \not\models C \sqsubseteq D$ .

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### A Weakening Relation ≻<sup>sub</sup>

$$C \sqsubseteq D \succ^{sub} C' \sqsubseteq D' \text{ if } C' = C, \ D \sqsubset D', \text{ and } \{C' \sqsubseteq D'\} \not\models C \sqsubseteq D.$$

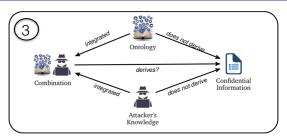
Employing both, maximally strong weakenings can be effectively computed

 $D \sqsubset^{syn} D' \Rightarrow$  removing occurrences of subconcepts of D.

#### A Weakening Relation ≻<sup>syn</sup>

$$C \sqsubseteq D \succ^{syn} C' \sqsubseteq D'$$
 if  $C' = C$  and  $D \sqsubseteq^{syn} D'$ , and  $\{C' \sqsubseteq D'\} \not\models C \sqsubseteq D$ .

# Problem 3: Privacy-Preserving Ontology Publishing (PPOP)







# PPOP for $\mathcal{EL}$ Ontologies ([DL 2018], [JELIA 2019], [KI 2019])

Restricting the ontology:

- ullet  $\mathcal{EL}$  Instance Stores &  $\mathcal{EL}$  ABoxes (No TBoxes)
- Instance Stores: Ontologies without individual relationships

### PPOP for $\mathcal{EL}$ Instance Stores



 $\mathcal{EL}$  Instance Stores without TBox



 $C_1(a), C_2(a)$  implies  $(C_1 \sqcap C_2)(a)$ 

only one concept assertion speaking about one individual





Published Information (an  $\mathcal{EL}$  Concept C)



Attacker's Knowledge

(an  $\mathcal{EL}$  /  $\mathcal{FL}_0$  /  $\mathcal{FLE}$ Concept E)



Confidential Information (a finite set of  $\mathcal{EL}$  concepts)  $\{D_1, \ldots, D_p\}$ 

### Confidential Information $P = \{D\}$ about LINDA



 $D = Patient \sqcap \exists seenBy.(Doctor \sqcap \exists worksIn.Oncology)$ 

#### Original Published Information C about LINDA



 $C = Patient \sqcap Female$  $\sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$ 

Note *C* is not **compliant with** *D* 

#### Confidential Information $P = \{D\}$ about LINDA



 $D = \textit{Patient} \sqcap \exists \textit{seenBy}. (\textit{Doctor} \sqcap \exists \textit{worksIn}. \textit{Oncology})$ 

### Original Published Information C about LINDA



 $C = Patient \sqcap Female$  $\sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$ 

Note *C* is not **compliant with** *D* 

#### Modification



 $\textit{C}_1 = \textit{Female} \, \sqcap \, \exists \textit{seenBy}. (\textit{Doctor} \, \sqcap \, \textit{Male} \, \sqcap \, \exists \textit{worksIn}. \textit{Oncology})$ 

Note  $C \sqsubseteq C_1$  and  $C_1$  complies with D

#### Confidential Information $P = \{D\}$ about LINDA



 $D = \textit{Patient} \sqcap \exists \textit{seenBy}. (\textit{Doctor} \sqcap \exists \textit{worksIn}. \textit{Oncology})$ 

### Original Published Information C about LINDA



 $C = Patient \sqcap Female$  $\sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$ 

Note C is not **compliant with** D

#### $\mathcal{EL}$ -Attacker is Coming!



 $\textit{C}_1 = \textit{Female} \sqcap \exists \textit{seenBy}. (\textit{Doctor} \sqcap \textit{Male} \sqcap \exists \textit{worksIn}. \textit{Oncology})$ 



He knows Patient(LINDA)

#### Confidential Information $P = \{D\}$ about LINDA



 $D = \textit{Patient} \sqcap \exists \textit{seenBy}. (\textit{Doctor} \sqcap \exists \textit{worksIn}. \textit{Oncology})$ 

### Original Published Information C about LINDA



 $C = Patient \sqcap Female$ 

 $\ \sqcap \ \exists seenBy. (\textit{Doctor} \sqcap \textit{Male} \sqcap \exists \textit{worksIn}. \textit{Oncology})$ 

Note C is not **compliant with** D

#### Linked and Revealed!



 $C_1' = Female \sqcap \exists seenBy. (Doctor \sqcap Male \sqcap \exists worksIn. Oncology)$  $\sqcap Patient$ 

Note D(LINDA) is **revealed** and  $C_1$  is not  $\mathcal{EL}$ -safe for D

### Confidential Information $P = \{D\}$ about LINDA



 $D = \textit{Patient} \sqcap \exists \textit{seenBy}. (\textit{Doctor} \sqcap \exists \textit{worksIn}. \textit{Oncology})$ 

#### Original **Published Information** C about LINDA



 $C = Patient \sqcap Female$  $\sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$ 

Note *C* is not **compliant with** *D* 

#### Modification



 $C_2 = Female \sqcap \exists seenBy. (Doctor \sqcap Male \sqcap \exists worksIn. \top)$  $\sqcap \exists seenBy. (Male \sqcap worksIn. Oncology)$ 

 $C_2$  is  $\mathcal{EL}$ -safe for D

### Confidential Information $P = \{D\}$ about LINDA



 $D = \textit{Patient} \sqcap \exists \textit{seenBy}.(\textit{Doctor} \sqcap \exists \textit{worksIn}.\textit{Oncology})$ 

### Original Published Information C about LINDA



 $C = Patient \sqcap Female$  $\sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$ 

Note *C* is not **compliant with** *D* 

### $\mathcal{FL}_0$ -Attacker is Coming!



 $C_2 = Female \sqcap \exists seenBy. (Doctor \sqcap Male \sqcap \exists worksIn. \top)$  $\sqcap \exists seenBy. (Male \sqcap worksIn. Oncology)$ 



He knows ( $Patient \sqcap \forall seenBy. \forall worksIn. Oncology$ )(LINDA)

#### Confidential Information $P = \{D\}$ about LINDA



 $D = \textit{Patient} \sqcap \exists \textit{seenBy}.(\textit{Doctor} \sqcap \exists \textit{worksIn}.\textit{Oncology})$ 

#### Original **Published Information** C about LINDA



```
C = Patient \sqcap Female

\sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)
```

Note C is not **compliant with** D

#### Linked and Revealed!



```
C_2' = Female \sqcap \exists seenBy. (Doctor \sqcap Male \sqcap \exists worksIn. \top)

\sqcap \exists seenBy. (Male \sqcap worksIn. Oncology)

\sqcap Patient \sqcap \forall seenBy. \forall worksIn. Oncology
```

D(LINDA) is revealed again and  $C_2$  is not  $\mathcal{FL}_0$ -safe for D

#### **Confidential Information** $P = \{D\}$ about *LINDA*



 $D = \textit{Patient} \sqcap \exists \textit{seenBy}. (\textit{Doctor} \sqcap \exists \textit{worksIn}. \textit{Oncology})$ 

### Original Published Information C about LINDA



 $C = Patient \sqcap Female$  $\sqcap \exists seenBy.(Doctor \sqcap Male \sqcap \exists worksIn.Oncology)$ 

Note *C* is not **compliant with** *D* 

#### Modification



 $C_3 = Female \sqcap Patient \sqcap \exists seenBy.(Doctor \sqcap Male)$ 

 $C_3$  is  $\mathcal{FL}_0$ -safe for D

## Decision & Computational Problems for Instance Stores

Given  $\mathcal{L} \in \{\mathcal{EL}, \mathcal{FL}_0, \mathcal{FLE}\}$ , a published information ( $\mathcal{EL}$  concept)  $\mathcal{C}$ , an  $\mathcal{EL}$  confidential information  $\mathcal{P}$ .

#### **Decision Problems**

- Compliance:
  - Is an  $\mathcal{EL}$  concept C compliant with  $\mathcal{P}$ ?
- L-Safety:

Is an  $\mathcal{EL}$  concept C  $\mathcal{L}$ -safe for  $\mathcal{P}$ ?

OptCom:

Is an  $\mathcal{EL}$  concept  $C_1$  an optimal compliant generalization of C w.r.t.  $\mathcal{P}$ ?

• *L*-Optimality:

Is an  $\mathcal{EL}$  concept  $C_1$  an optimal  $\mathcal{L}$ -safe generalization of C for  $\mathcal{P}$ ?

#### Note

Optimal: For all  $C_2$ , if  $C_2 \sqsubset C_1$ , then  $C_2$  is not (compliant)  $\mathcal{L}$ -safe w.r.t.  $\mathcal{P}$ .

## Decision & Computational Problems for Instance Stores

Given  $\mathcal{L} \in \{\mathcal{EL}, \mathcal{FL}_0, \mathcal{FLE}\}$ , a published information ( $\mathcal{EL}$  concept)  $\mathcal{C}$ , an  $\mathcal{EL}$  confidential information  $\mathcal{P}$ .

#### **Decision Problems**

- Compliance: Is an  $\mathcal{EL}$  concept C compliant with  $\mathcal{P}$ ?
- L-Safety: Is an EL concept C L-safe for P?
- OptCom: Is an  $\mathcal{EL}$  concept  $C_1$  an optimal compliant generalization of C w.r.t.  $\mathcal{P}$ ?
- $\mathcal{L}$ -Optimality: Is an  $\mathcal{EL}$  concept  $C_1$  an optimal  $\mathcal{L}$ -safe generalization of C for  $\mathcal{P}$ ?

### Computational Problem

Find an  $\mathcal{EL}$  concept  $C_1$  s.t  $C_1$  is an optimal (compliant)  $\mathcal{L}$ -safe generalization of C for  $\mathcal{P}$ !

### Complexity Results on PPOP for $\mathcal{EL}$ Instance Stores

Compliance is in PTime, whereas OptCom is in coNP, but Dual-hard.

Decision Problems	$\mathcal{L} = \mathcal{E}\mathcal{L}$	$\mathcal{L} = \mathcal{F}\mathcal{L}_0$	$\mathcal{L} = \mathcal{F} \mathcal{L} \mathcal{E}$
$\mathcal{L}$ -safety	PTime	PTime	PTime
$\mathcal{L}$ -optimality	coNP and Dual-hard	coNP and Dual-hard	PTime

Table: Complexity results of  $\mathcal{L}$ -safety and  $\mathcal{L}$ -optimality on PPOP for  $\mathcal{EL}$  instance stores

Optimal Compliance Generalization(s) can be computed in ExpTime.

Computational Problems	$\mathcal{L} = \mathcal{E}\mathcal{L}$	$\mathcal{L} = \mathcal{F}\mathcal{L}_0$	$\mathcal{L} = \mathcal{FLE}$
Optimal $\mathcal{L}$ -safe Generalization(s)	ExpTime	ExpTime	PTime

Table: Complexity of computing one/all optimal  $\mathit{Q}$ -safe generalizations for  $\mathcal{P}$ 

### PPOP for $\mathcal{EL}$ ABoxes

Including relationships between individuals in  $\mathcal{EL}$  ABoxes.



Published Information (an  $\mathcal{EL}$  ABox)



Attacker's

Knowledge (an  $\mathcal{EL}$  ABox)



Confidential Information (an  $\mathcal{EL}$  concept or a conjunctive query)

### PPOP for $\mathcal{EL}$ ABoxes

Including relationships between individuals in  $\mathcal{EL}$  ABoxes.



Published Information (an  $\mathcal{EL}$  ABox)



Attacker's Knowledge (an  $\mathcal{EL}$  ABox)



Confidential Information (an  $\mathcal{EL}$  concept or a conjunctive query)

Given an  $\mathcal{EL}$  ABox  $\mathcal{A}$ , and a confidential information  $\mathcal{P}$  that is either an **instance** query  $(\mathcal{EL}$  concept)  $\mathcal{D}$  or a **conjunctive query** q.

- A is **compliant** with D iff  $A \not\models D(a)$  for all individuals a.
- $\mathcal{A}$  is **compliant** with q iff  $\mathcal{A} \not\models q(\vec{a})$  for all tuples  $\vec{a}$  of individuals.
- $\mathcal{A}$  is **safe** for  $\mathcal{P}$  iff for all (attackers' knowledge)  $\mathcal{A}'$  complying with  $\mathcal{P}$ ,  $\mathcal{A} \cup \mathcal{A}'$  complies with  $\mathcal{P}$

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How to modify  $\mathcal{EL}$  ABoxes?



#### A-anonymizer f

 ${\mathcal A}$ 

- 1. Replace individuals with new anonymous individuals
- 2. Two different individuals cannot be replaced by the same anonymous individual
- 3. Generalizing concepts



### A-anonymizer f

- 1. Replace individuals with new anonymous individuals
- 2. Two different individuals cannot be replaced by the same anonymous individual
- 3. Generalizing concepts

### **ABox Anonymization**

```
\mathcal{A}_0 := \{ \ Doctor \ \sqcap \ \exists worksIn.Oncology(LINDA), \ seenBy(BOB, LINDA) \} \ \downarrow f_1 \checkmark \ \mathcal{A}_1 := \{ \ Doctor \ \sqcap \ \exists worksIn.Oncology(y), \ seenBy(x, LINDA) \}
```



### A-anonymizer f

- 1. Replace individuals with new anonymous individuals
- 2. Two different individuals cannot be replaced by the same anonymous individual
- 3. Generalizing concepts

### **ABox Anonymization**



### A-anonymizer f

- 1. Replace individuals with new anonymous individuals
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- 3. Generalizing concepts

### **ABox Anonymization**

# Optimality in Anonymizations



#### A-anonymizer f

- 1. Replace individuals with new anonymous individuals
- 2. Two different individuals cannot be replaced by the same anonymous individual
- 3. Generalizing concepts

### Measuring Optimality

An A-anonymizer  $f_2$  is **more informative than** an A-anonymizer  $f_1$   $(f_2 > f_1)$  if  $f_2$  can be obtained from  $f_1$  by:

- keeping more known individuals
- identifying more distinct anonymous individuals
- ullet specializing more  $\mathcal{EL}$  concepts



### Decision Problems on PPOP for $\mathcal{EL}$ ABoxes

Given an  $\mathcal{EL}$  ABox  $\mathcal{A}$ , an  $\mathcal{EL}$  concept D, and an  $\mathcal{A}$ -anonymizer f,

- Compliance<sub>IQ</sub>, Safety<sub>IQ</sub>, and
- Optimal-Compliance<sub>IQ</sub> (Optimal-Safety<sub>IQ</sub>) asks
  - if f(A) is compliant with (safe for) D and
  - for all  $\mathcal{A}$ -anonymizers f', if f' > f, then  $f'(\mathcal{A})$  is not compliant with (safe for) D

Analogous for Compliance<sub>CQ</sub>, Safety<sub>CQ</sub>, Optimal-Compliance<sub>CQ</sub>, and Optimal-Safety<sub>CQ</sub>, where the policy is a CQ

### Decision Problems on PPOP for $\mathcal{EL}$ ABoxes

Given an  $\mathcal{EL}$  ABox  $\mathcal{A}$ , an  $\mathcal{EL}$  concept D, and an  $\mathcal{A}$ -anonymizer f,

- Compliance<sub>IQ</sub>, Safety<sub>IQ</sub>, and
- ullet Optimal-Compliance<sub>IQ</sub> (Optimal-Safety<sub>IQ</sub>) asks
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Analogous for Compliance<sub>CQ</sub>, Safety<sub>CQ</sub>, Optimal-Compliance<sub>CQ</sub>, and Optimal-Safety<sub>CQ</sub>, where the policy is a CQ

Decision Problems	X = IQ	X = CQ
$Compliance_X$	PTime	coNP-complete
$Safety_X$	PTime	$\Pi_2^p$ and DP-hard
Optimal-Compliance $_X$	coNP and Dual-hard	$\Pi_2^p$ and DP-hard
Optimal-Safety $_X$	coNP and Dual-hard	$\Pi_3^p$ and DP-hard

Table: Complexity Results on PPOP in  $\mathcal{EL}$  ABoxes

#### Conclusions

#### The Identity Problem:

- Non trivial for DLs with equality power
- Introducing variants of the identity problem
- Reduction to classical reasoning in DLs

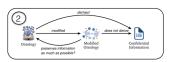
#### Gentle Repair:

- Introducing a framework for repair via axiom weakening
- Weakening relations
- ullet Weakening axioms in  $\mathcal{EL}$

### Privacy-Preserving Ontology Publishing:

- ullet PPOP for  $\mathcal{EL}$  Instance Stores
- PPOP for EL ABoxes
- Applying the concepts of compliance, safety, and optimality in both settings







#### Future Work

#### The Identity Problem:

- Formalizing the "real" definition of k-Anonymity
- Adding probability to the setting



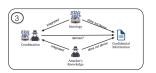
#### Gentle Repair:

- Choosing which axioms to be repaired
- Which maximally strong weakening is the best?
- Weakening relations for other DLs



### Privacy-Preserving Ontology Publishing:

- Computing the optimal compliant (safe) anonymization
- Finding a more gentle weakening relation for ABox anonymization
- Including TBox/attackers' meta knowledge? (Bonatti et. al., 2013)



#### **Publications**

- Franz Baader, Daniel Borchmann, and Adrian Nuradiansyah, Preliminary Results on the Identity Problem in Description Logic Ontologies, DL 2017, Montpellier, 2017.
- Franz Baader, Daniel Borchmann, and Adrian Nuradiansyah, The Identity
   Problem in Description Logic Ontologies and Its Applications to View-Based
   Information Hiding, JIST 2017, Gold Coast, 2017.
- Franz Baader, Francesco Kriegel, Adrian Nuradiansyah, and Rafael Peñaloza, Making Repairs in Description Logics More Gentle, KR 2018, Tempe, 2018.
- Franz Baader and Adrian Nuradiansyah, Towards Privacy-Preserving Ontology Publishing, DL 2018, Tempe, 2018.
- Franz Baader, Francesco Kriegel, and Adrian Nuradiansyah, Privacy-Preserving Ontology Publishing for && Instance Stores, JELIA 2019, Rende, 2019.
- Franz Baader and Adrian Nuradiansyah, Mixing Description Logics in Privacy-Preserving Ontology Publishing, KI 2019, Kassel, 2019.

Adrian Nuradiansyah PhD Defense September 27, 2019 30 / 32

#### Research Visits and Awards

#### Research Visits:

- Visiting Prof. Rafael Peñaloza at Free University of Bozen-Bolzano, March 1-May 16, 2018.
- Visiting Prof. Bernardo Cuenca Grau at the University of Oxford, UK, April 1 - June 30, 2019.

#### Awards:

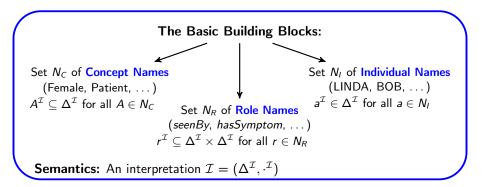
- The Best Student Paper Award at the 7th Joint International Semantic Technology Conference (JIST 2017) at Gold Coast, Australia.
- Shortlisted for The Best Paper Award at the Künstliche Intelligenz Conference (KI 2019) at Kassel, Germany.

# Thank You



# Backup Slides

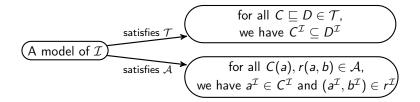
### Semantics of DLs



## Semantics of DL Concepts

Name	Syntax	Example
Тор	Т	$\Delta^{\mathcal{I}}$
Concept Name	Α	$A^{\mathcal{I}}$
Conjunction	$C \sqcap D$	$C^{\mathcal{I}}\cap D^{\mathcal{I}}$
Disjunction	$C \sqcup D$	$C^{\mathcal{I}} \cup D^{\mathcal{I}}$
Existential Restriction	∃r.C	$\{d \in \Delta^{\mathcal{I}} \mid \exists e \in \Delta^{\mathcal{I}} : (d, e) \in r^{\mathcal{I}} \land e \in C^{\mathcal{I}}\}$
Universal Restriction	∀r.C	$\{d \in \Delta^{\mathcal{I}} \mid \forall e \in \Delta^{\mathcal{I}} : (d, e) \in r^{\mathcal{I}} \text{ implies } e \in C^{\mathcal{I}}\}$
Negation	$\neg C$	$\Delta^{\mathcal{I}} \setminus C^{\mathcal{I}}$
(One of) Nominal	$\{a_1,\ldots,a_n\}$	$\{a_1^{\mathcal{I}},\ldots,a_n^{\mathcal{I}}\}$

## Semantics of DL Ontologies



### The Identity Problem in Rôle-Based Access Control

#### Given an ontology $\mathfrak{O}_I$



At rôle  $\hat{r}_1$  - queries through  $\mathfrak{O}_{\hat{r}_1} \subseteq \mathfrak{O}_I$  switch . . . switch - obtains View  $V_{\hat{r}_1}$ 

At rôle  $\hat{r}_k$  - queries through  $\mathfrak{O}_{\hat{r}_k} \subseteq \mathfrak{O}_I$ 

- obtains View  $V_{\hat{r}_k}$ 

Is the identity of an anonymous x hidden w.r.t.  $V_{\hat{r}_1}, \ldots, V_{\hat{r}_k}$ ?

(The View-Based Identity (VBI) Problem)

### The Identity Problem in Rôle-Based Access Control

#### Given an ontology $\mathfrak{O}_I$



```
At rôle \hat{r}_1 - queries through \mathfrak{O}_{\hat{r}_1} \subseteq \mathfrak{O}_I switch - switch - queries through \mathfrak{O}_{\hat{r}_k} \subseteq \mathfrak{O}_I - obtains View V_{\hat{r}_k}
```

Is the identity of an anonymous x hidden w.r.t.  $V_{\hat{t}_1}, \dots, V_{\hat{t}_k}$ ? (The View-Based Identity (VBI) Problem)

Similar scenarios studied in (Stouppa et al., 2009) or (Calvanese et. al., 2008).

- Only consider instance and subsumption queries
- View is a finite set of pairs of gueries and the answers

#### Here, we

- Consider subsumption queries:  $C \sqsubseteq D$ , conjunctive queries:  $\exists \vec{y}.conj(\vec{x},\vec{y})$ , and
- $N_I = N_{KI} \cup N_{AI}$ , sets of known and anonymous individuals, respectively.
- Concentrate on hiding the identity of anonymous individuals  $(idn(x, \mathfrak{O}) := \{a \in N_{KI} \mid \mathfrak{O} \models x = a\})$



### The Identity Problem in Rôle-Based Access Control

#### Given an ontology $\mathfrak{O}_I$



- At rôle  $\hat{r}_1$  At rôle  $\hat{r}_k$
- queries through  $\mathfrak{O}_{\hat{r}_{\mathbf{i}}}\subseteq \mathfrak{O}_{I}$  switch . . . switch queries through  $\mathfrak{O}_{\hat{r}_{k}}\subseteq \mathfrak{O}_{I}$
- obtains View  $V_{\hat{r}_{\! 1}}$  obtains View  $V_{\hat{r}_{\! k}}$

Is the identity of an anonymous x hidden w.r.t.  $V_{\hat{r}_1}, \dots, V_{\hat{r}_k}$ ? (The View-Based Identity (VBI) Problem)

#### Reduction

The VBI problem can be reduced to the identity problem for *some* DLs with equality power

## Maximally Strong Weakening Axioms

Replace  $\beta$  with exactly one weaker  $\gamma$  s.t.

$$\mathfrak{D}_s \cup (J_i \setminus \{\beta\}) \cup \{\gamma\} \not\models \alpha \text{ for } i = 1, \dots, k$$

If  $\gamma$  is a tautology, then it is the same as classical repair.

To make this repair as gentle as possible,  $\gamma$  should be maximally strong

$$\mathfrak{O}_s \cup (J_i \setminus \{\beta\}) \cup \{\gamma\} \not\models \alpha$$
but for all  $\delta$  such that  $\beta \succ \delta \succ \gamma$ , we have 
$$\mathfrak{O}_s \cup (J_i \setminus \{\beta\}) \cup \{\delta\} \models \alpha$$

## Maximally Strong Weakening Axioms

Replace  $\beta$  with exactly one weaker  $\gamma$  s.t.

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 but for all  $\delta$  such that  $\beta \succ \delta \succ \gamma$ , we have 
$$\mathfrak{D}_{s} \cup (J_{i} \setminus \{\beta\}) \cup \{\delta\} \models \alpha$$

#### **Proposition**

If  $\succ$  is well-founded, **one-step generated**, and **finitely branching**, then maximally strong weakenings can be effectively computed

## Maximally Strong Weakening Axioms

To make this repair as gentle as possible,  $\gamma$  should be maximally strong

$$\mathfrak{O}_s \cup (J_i \setminus \{\beta\}) \cup \{\gamma\} \not\models \alpha$$
 but for all  $\delta$  such that  $\beta \succ \delta \succ \gamma$ , we have 
$$\mathfrak{O}_s \cup (J_i \setminus \{\beta\}) \cup \{\delta\} \models \alpha$$

#### **Proposition**

If  $\succ$  is well-founded, one-step generated, and finitely branching, then maximally strong weakenings can be effectively computed

#### One-Step Generated:

if  $\beta \succ \gamma$ , then we cannot refine all weakening chains between  $\beta$  and  $\gamma$ 

Finitely branching: The set  $\{\gamma \mid \beta \succ_1 \gamma\}$  is

### A Weakening Relation ≻<sup>sub</sup> [BaKrNuPe, CoRR 2018]

$$C \sqsubseteq D \succ^{sub} C' \sqsubseteq D'$$
 if  $C' = C$ ,  $D \sqsubset D'$ , and  $\{C' \sqsubseteq D'\} \not\models C \sqsubseteq D$ .

#### A Weakening Relation ≻<sup>syn</sup> [BaKrNuPe, CoRR 2018]

$$C \sqsubseteq D \succ^{syn} C' \sqsubseteq D'$$
 if  $C' = C$  and  $D \sqsubseteq^{syn} D'$ , and  $\{C' \sqsubseteq D'\} \not\models C \sqsubseteq D$ .

### A Weakening Relation ≻<sup>sub</sup> [BaKrNuPe, CoRR 2018]

$$C \sqsubseteq D \succ^{sub} C' \sqsubseteq D'$$
 if  $C' = C, \ D \sqsubset D'$ , and  $\{C' \sqsubseteq D'\} \not\models C \sqsubseteq D$ .

- Employing both, maximally strong weakenings can be effectively computed
- Both weakening relations are well-founded, complete, one-step generated, and finitely branching

### A Weakening Relation $\succ^{syn}$ [BaKrNuPe, CoRR 2018]

$$C \sqsubseteq D \succ^{syn} C' \sqsubseteq D'$$
 if  $C' = C$  and  $D \sqsubseteq^{syn} D'$ , and  $\{C' \sqsubseteq D'\} \not\models C \sqsubseteq D$ .

### A Weakening Relation ≻<sup>sub</sup> [BaKrNuPe, CoRR 2018]

$$C \sqsubseteq D \succ^{sub} C' \sqsubseteq D' \text{ if } C' = C, \ D \sqsubset D', \text{ and } \{C' \sqsubseteq D'\} \not\models C \sqsubseteq D.$$

- $\bullet \succ^{sub}$  is not polynomial
- ullet | D' | can be exponentially bounded by | D |
- IndonesianPolitician  $\sqsubseteq \exists receives. (Parcel \sqcap Deluxe)$  weaken IndonesianPolitician  $\sqsubseteq \exists receives. Parcel \sqcap \exists receives. Deluxe$

### A Weakening Relation ≻<sup>syn</sup> [BaKrNuPe, CoRR 2018]

$$C \sqsubseteq D \succ^{syn} C' \sqsubseteq D'$$
 if  $C' = C$  and  $D \sqsubseteq^{syn} D'$ , and  $\{C' \sqsubseteq D'\} \not\models C \sqsubseteq D$ .

### A Weakening Relation $\succ^{sub}$ [BaKrNuPe, CoRR 2018]

$$C \sqsubseteq D \succ^{sub} C' \sqsubseteq D' \text{ if } C' = C, \ D \sqsubset D', \text{ and } \{C' \sqsubseteq D'\} \not\models C \sqsubseteq D.$$

- $\succ^{syn}$  is linear (|D| > |D'|)
- IndonesianPolitician 
   □ ∃receives.(Parcel □ Deluxe) weaken
   IndonesianPolitician □ ∃receives.Parcel or
   IndonesianPolitician □ ∃receives.Deluxe

### A Weakening Relation $\succ^{syn}$ [BaKrNuPe, CoRR 2018]

$$C \sqsubseteq D \succ^{syn} C' \sqsubseteq D'$$
 if  $C' = C$  and  $D \sqsubseteq^{syn} D'$ , and  $\{C' \sqsubseteq D'\} \not\models C \sqsubseteq D$ .

## Formalizing Sensitive Information in $\mathcal{EL}$ Instance Stores

Given an  $\mathcal{EL}$  concept C (published information) and an  $\mathcal{EL}$  policy  $\mathcal{P}$  Given a DL  $\mathcal{L} \in \{\mathcal{EL}, FLO, FLE\}$ .

### Compliance and Safety

- 1. an  $\mathcal{L}$  concept C' is **compliant with**  $\mathcal{P}$  if  $C' \not\sqsubseteq D_i$  for all i = 1, ..., p,
- 2. an  $\mathcal{EL}$  concept C' is
  - $\mathcal{L}$ -safe for  $\mathcal{P}$  if for all  $\mathcal{L}$  concepts E (attackers' knowledge) that are compliant with  $\mathcal{P}$ ,  $C' \sqcap E$  is also compliant with  $\mathcal{P}$ ,

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  - a  $\mathcal{L}$ -safe generalization of C for  $\mathcal{P}$  if  $C \sqsubseteq C'$  and C' is  $\mathcal{L}$ -safe for  $\mathcal{P}$
  - ullet an **optimal**  $\mathcal{L}$ -safe generalization of C for  $\mathcal{P}$  if
    - C' is a  $\mathcal{L}$ -safe generalization of C for  $\mathcal{P}$  and
    - there is no  $\mathcal{L}$ -safe generalization C'' of C for  $\mathcal{P}$  s.t.  $C'' \sqsubseteq C'$ .

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Optimal Compliance Generalization(s) can be computed in **ExpTime**.

Computational Problems	<b>Q</b> = ∃	$\mathbf{Q} = \forall$	$\mathbf{Q} = \forall \exists$
Optimal <i>Q</i> -safe Generalization(s)	ExpTime	ExpTime	PTime

#### Reasons:

- Given an  $\mathcal{EL}$  concept D, con(D) is the set of all atoms  $(A \text{ or } \exists r.D')$  in the top-level conjunction of D.
- Computing all minimal hitting sets of  $con(D_1), \ldots, con(D_p)$ , where  $\mathcal{P} = \{D_1, \ldots, D_p\}$  recursively on the role depth of the published information C

Decision Problems	<b>Q</b> = ∃	$\mathbf{Q} = \forall$	$\mathbf{Q} = \forall \exists$
Q-safety	PTime	PTime	PTime
Q-optimality	<b>coNP</b> and Dual -hard	<b>coNP</b> and Dual-hard	PTime

#### Reasons:

- Check if  $C_1$  is an  $\forall$ -safe generalization of C for  $\mathcal P$
- Check if there is  $C_2$  s.t.  $C \sqsubseteq C_2 \sqsubset C_1$ , where  $C_2$  is a not  $\forall$ -safe generalization of C for  $\mathcal{P}$
- There is an NP algorithm to guess such concept  $C_2$  (Baader, Kriegel, Nuradiansyah in JELIA 2019)

Decision Problems	$\mathcal{L} = \mathcal{E}\mathcal{L}$	$\mathcal{L} = \mathcal{F}\mathcal{L}_0$	$\mathcal{L} = \mathcal{FLE}$
$\mathcal{L}$ -safety	PTime	PTime	PTime
$\mathcal{L}$ -optimality	coNP and <b>Dual-hard</b>	coNP and <b>Dual-hard</b>	PTime

Computational Problems	<b>Q</b> = ∃	$\mathbf{Q} = \forall$	<b>Q</b> = ∀∃
Optimal <i>Q</i> -safe Generalization(s)	ExpTime	ExpTime	PTime

#### Reasons:

- $\mathcal{EL}$  ( $\mathcal{FL}_0$ )-Optimality is coNP-hard? Don't know yet
- ullet There is a polynomial reduction of **Dual problem** to  $\mathcal{EL}$  ( $\mathcal{FL}_0$ )-Optimality

Given two **families of inclusion-comparable sets**  $\mathcal{G}$  and  $\mathcal{H}$ , Dual asks whether  $\mathcal{H}$  consists exactly of the minimal hitting sets of  $\mathcal{G}$ .

Decision Problems	<b>Q</b> = ∃	$\mathbf{Q} = \forall$	$\mathbf{Q} = \forall \exists$
Q-safety	PTime	PTime	PTime
Q-optimality	coNP* and Dual-hard	coNP and Dual-hard	PTime

Computational Problems	<b>Q</b> = ∃	$\mathbf{Q} = \forall$	<b>Q</b> = ∀∃
Optimal Q-safe	EvnTimo	ExpTime	PTime
Generalization(s)	Exprime	Exprime	Fillie

#### Reasons:

### $\forall \exists$ -Safety and $\forall \exists$ -Optimality

C is  $\forall \exists$ -safe for  $\mathcal{P}$  iff

- 1.  $A \notin con(C)$  for all concept names  $A \in con(D_1) \cup ... \cup con(D_p)$ , and
- 2. for all existential restrictions  $\exists r.D' \in \text{con}(D_1) \cup \ldots \cup \text{con}(D_p)$ , there is no concept of the form  $\exists r.E \in \text{con}(C)$

## Complexity Results on PPOP for $\mathcal{EL}$ ABoxes

Decision Problems	X = IQ	X = CQ
$Compliance_X$	PTime	coNP-complete
$Safety_X$	PTime	$\Pi_2^p$ and DP-hard
Optimal-Compliance $_X$	coNP and Dual-hard	$\Pi_2^p$ and DP-hard
Optimal-Safety $_X$	coNP and Dual-hard	$\Pi_3^p$ and DP-hard

#### Reasons:

### Characterizing Safety<sub>IQ</sub>

A is safe for D iff for all  $a \in N_{KI}$ ,

- if  $C(a) \in A$  and E is a subconcept of D, then C is  $\exists$ -safe for  $\{E\}$  and
- if  $r(a, u) \in \mathcal{A}$  and  $\exists r.D'$  is a subconcept of D, then  $u \notin N_{KI}$  and  $\mathcal{A}$  is safe for D' and u.

Checking this can also be done in PTime

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#### Reasons:

#### 1. Safety $_{CQ}$ :

- Considering all  $\mathcal{EL}$  ABoxes  $\mathcal{A}'$  (attacker's knowledge) whose size is linearly bounded in the size of the CQ q, and
- Call an NP oracle to check if  $\mathcal{A}'$  complies with q or  $\mathcal{A} \cup \mathcal{A}'$  does not comply with q.

#### 2. Optimal-Compliance<sub>CQ</sub> and Optimal-Safety<sub>CQ</sub>:

- Considering all A-anonymizers f' that are "adjacent" to f
   (no A-anonymizers f" in between f and f' w.r.t. informativeness order).
- Call an coNP  $(\Pi_2^p)$  oracle to check if f'(A) is compliant with (safe for) q.

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#### Reasons:

- No tight complexity found yet for them
- There is a polynomial reduction from Homomorphism-NoHomomorphism problem to each of them
  - Given connected directed graphs  $G_1$ ,  $G_2$ ,  $G_1'$ , and  $G_2'$ , check whether there is a homomorphism from  $G_1$  to  $G_2$  and no homomorphism from  $G_1'$  to  $G_2'$
- Homomorphism-NoHomomorphism is DP-complete and

$$\mathsf{DP} = \{ L \mid \exists L_1 \in \mathsf{NP} \land \exists L_2 \in \mathsf{coNP} \text{ s.t. } L = L_1 \cap L_2 \}$$